



Laura Bassi Centre of Expertise  
**Centre for Visual Analytics  
Science & Technology**

# Maybe... Maybe not: Uncertainty in Time-Oriented Data Visualization

Theresia Gschwandtner, Wolfgang Aigner

[www.cvast.tuwien.ac.at](http://www.cvast.tuwien.ac.at)



# Overview

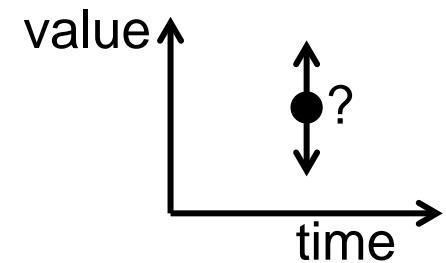
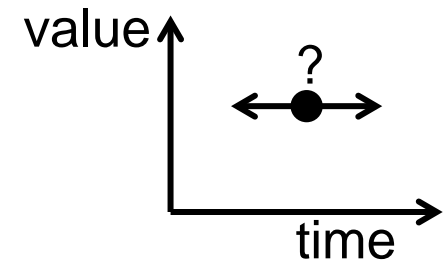
Characteristics of time

Modeling time

Visualizing time

Visualizing temporal uncertainty

Visualizing uncertainty of time-oriented data



# **CHARACTERISTICS OF TIME**



# Data Types

1-dimensional

2-dimensional

3-dimensional

Temporal

**= 4D space**  
**“the world we are living in”**

Multi-dimensional

Tree

Network

# Spatial + Temporal Dimensions

Every data element we measure is related and often only meaningful in context of **space + time**

*Example:* price of a computer

**where?**

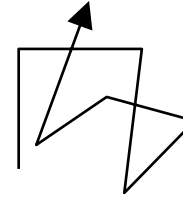
**when?**



# Differences between Space and Time

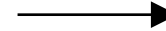
**Space** can be traversed “arbitrarily”

We can move back to where we came from



**Time** is unidirectional

We can't go back or forward in time

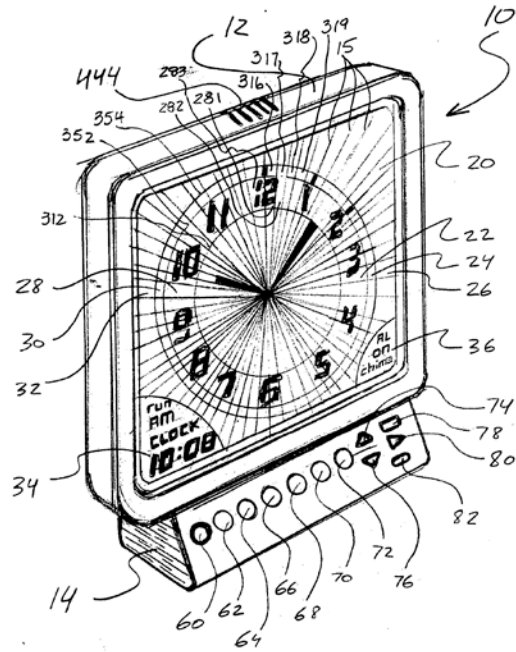


Humans have senses for perceiving **space**

Visually, touch

Humans don't have senses for perceiving **time**

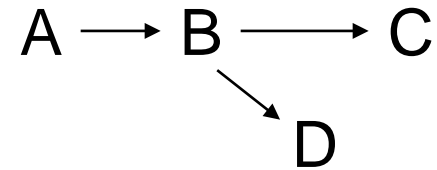
# Time has a Complex Structure



# Scale

## ordinal

*only order is known*



## discrete

*every element of time has a unique predecessor and successor*

comparable to Integer

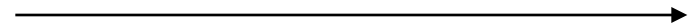


## continuous

*between any two elements in time there might be another one in between*

dense time

comparable to Float

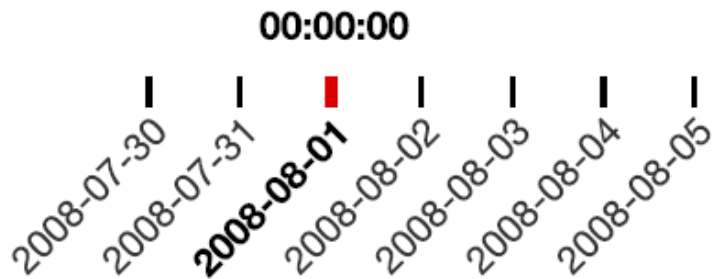




# Scope

## point-based

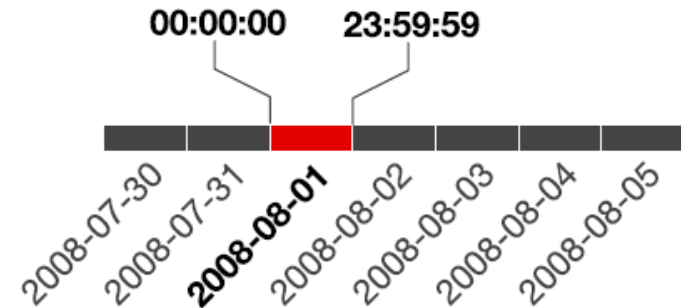
*example: August 1, 2008*



*no information is given in between two time points*

## interval-based

*example: August 1, 2008*



*each element covers a subsection of the time domain greater than zero*

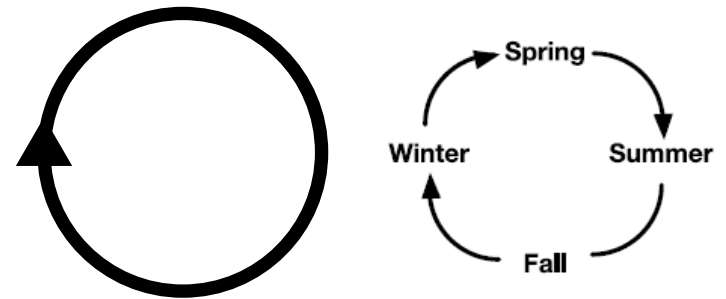
# Arrangement

linear



*each element of time has  
a unique predecessor  
and a unique successor*

cyclic



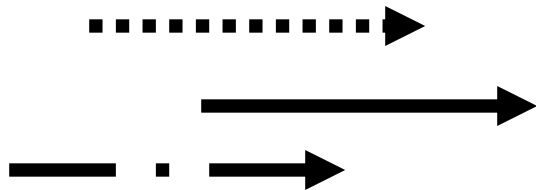
*summer is before winter,  
but winter is also before  
summer*

# Viewpoints

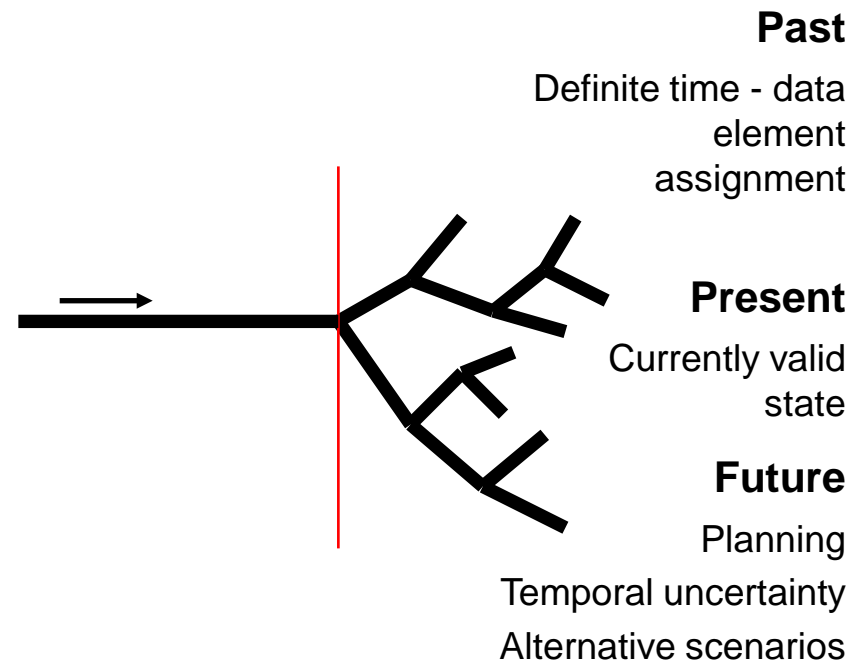
**ordered**



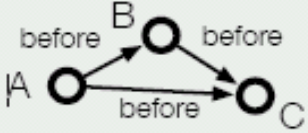
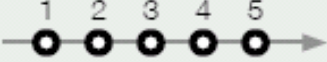






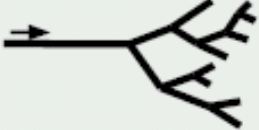

**multiple perspectives**



**branching**



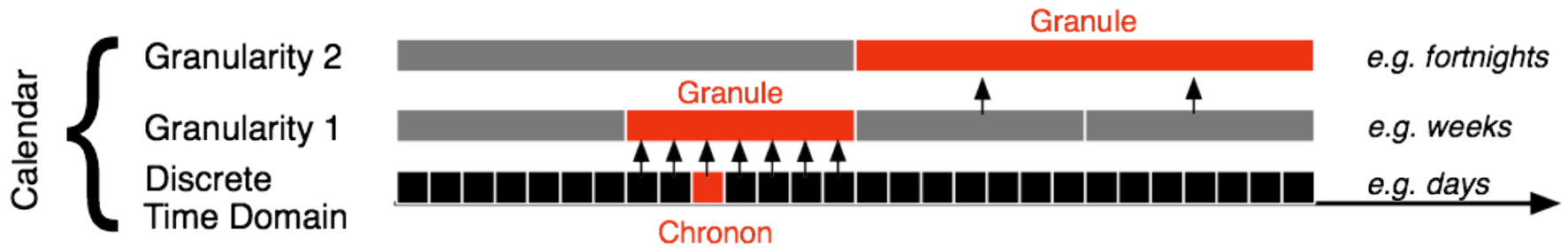
# Time Structure

scale	 <p>ordinal</p>	 <p>discrete</p>	 <p>continuous</p>
scope	 <p>point-based</p>	 <p>interval-based</p>	
arrangement	 <p>linear</p>	 <p>cyclic</p>	
viewpoint	 <p>ordered</p>	 <p>branching</p>	 <p>multiple perspectives</p>

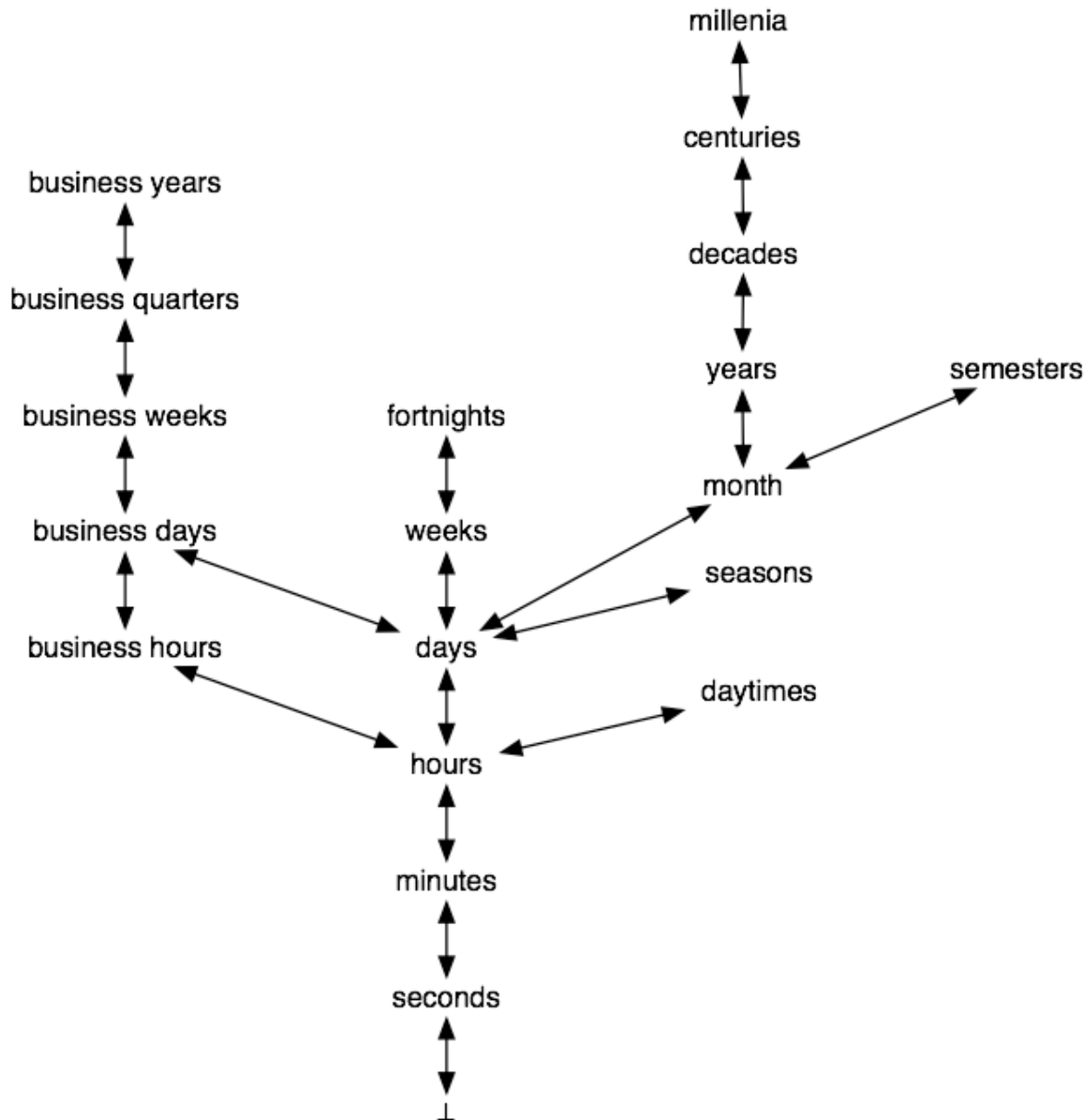
# MODELING TIME



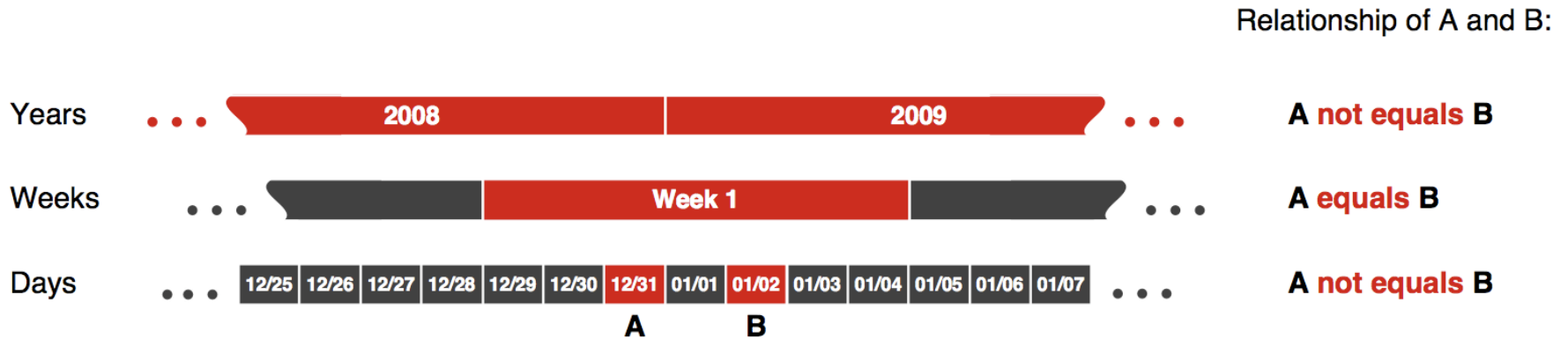
# Granularity



# Calendar



# Example: Granularity Paradoxon

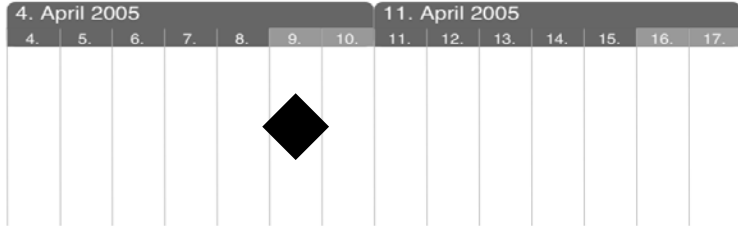




# Time Primitives

*anchored*

**instant** - single point in time



*unanchored*

**span** - duration of time



**interval** - duration between 2 instants



# Determinacy

## **determinate**

complete knowledge of temporal attributes

## **indeterminate**

incomplete knowledge of temporal attributes

no exact knowledge

*i.e. "time when the earth was formed"*

future planning

*i.e. "it will take 2-3 weeks"*

imprecise event times

*i.e. "one or two days ago"*

multiple granularities



# Temporal Uncertainty

[June 13, 2009; June 19, 2009]

minimum duration



maximum duration



possible beginning



possible ending



hours



days











2009-06-13  
2009-06-14  
2009-06-15  
2009-06-16  
2009-06-17  
2009-06-18  
2009-06-19

*Implicit indeterminacy when representing the interval [June 14, 2009; June 17, 2009] that is given at a granularity of **days** on a finer granularity of **hours***

# Modeling Time

## Abstractions

granularity & calendars	 none	 single	 multiple
time primitives	 instant	 interval	 span
determinacy	 determinate	 indeterminate	

# VISUALIZING TIME



# Visual Mapping of Time

## Dynamic: *Time* → *Time (Animation)*

probably the most natural form of mapping  
no “conversion” of concepts needed in between  
well suited for

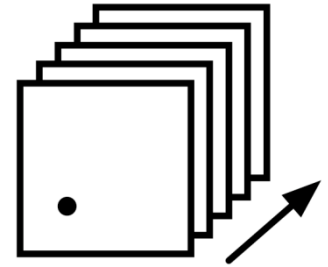
keeping track of changes

following trends and movements

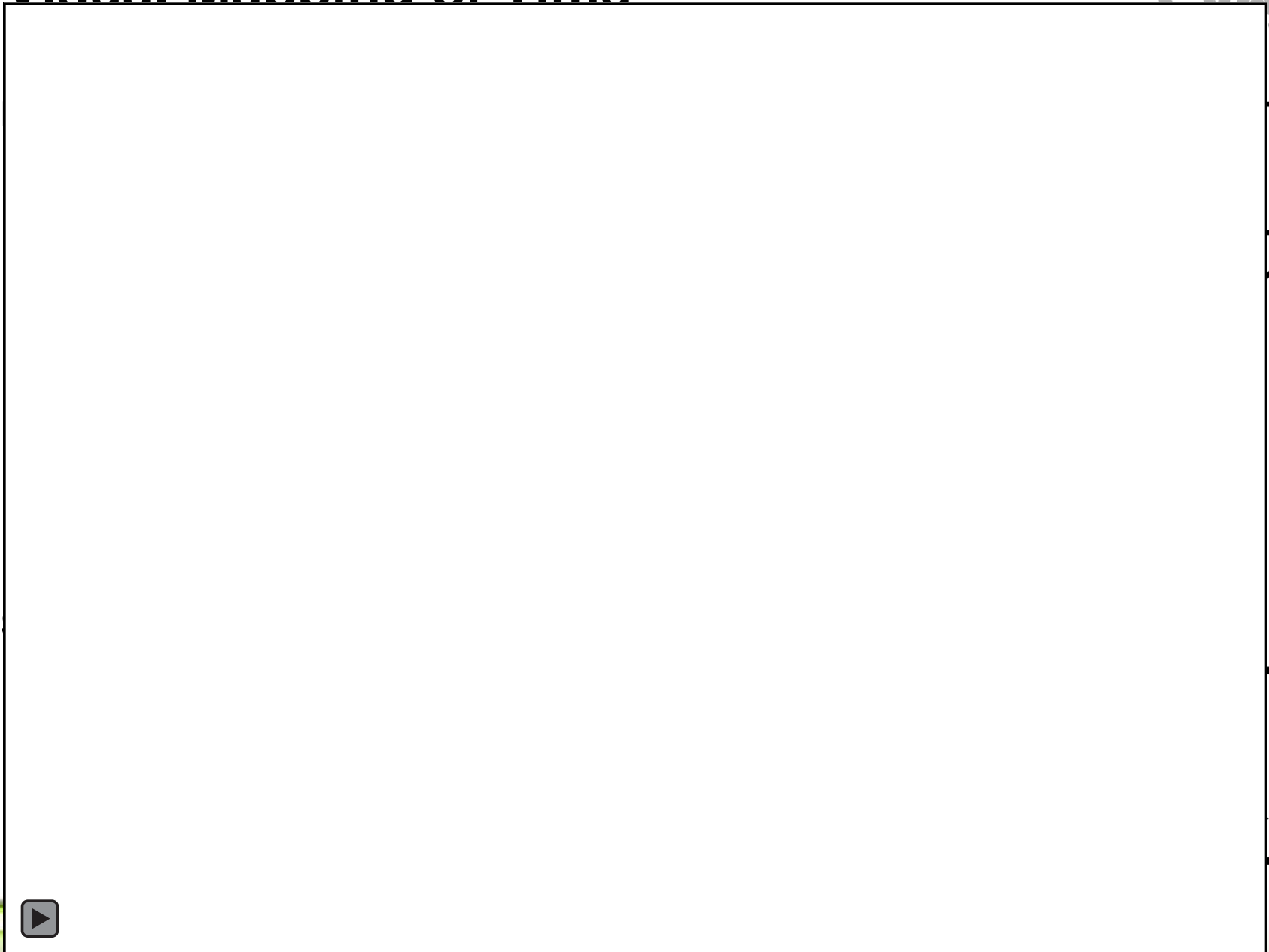
not well suited for

analytic and explorative tasks

no direct comparison of parameters between different points in time is possible



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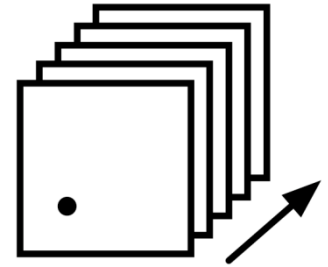
keeping track of changes

following trends and movements

not well suited for

analytic and explorative tasks

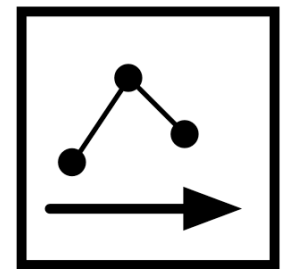
no direct comparison of parameters between different points in time is possible



## Static: *Time* → *Space*

mapping of time to visual features

direct comparison of parameters between different points in time is possible

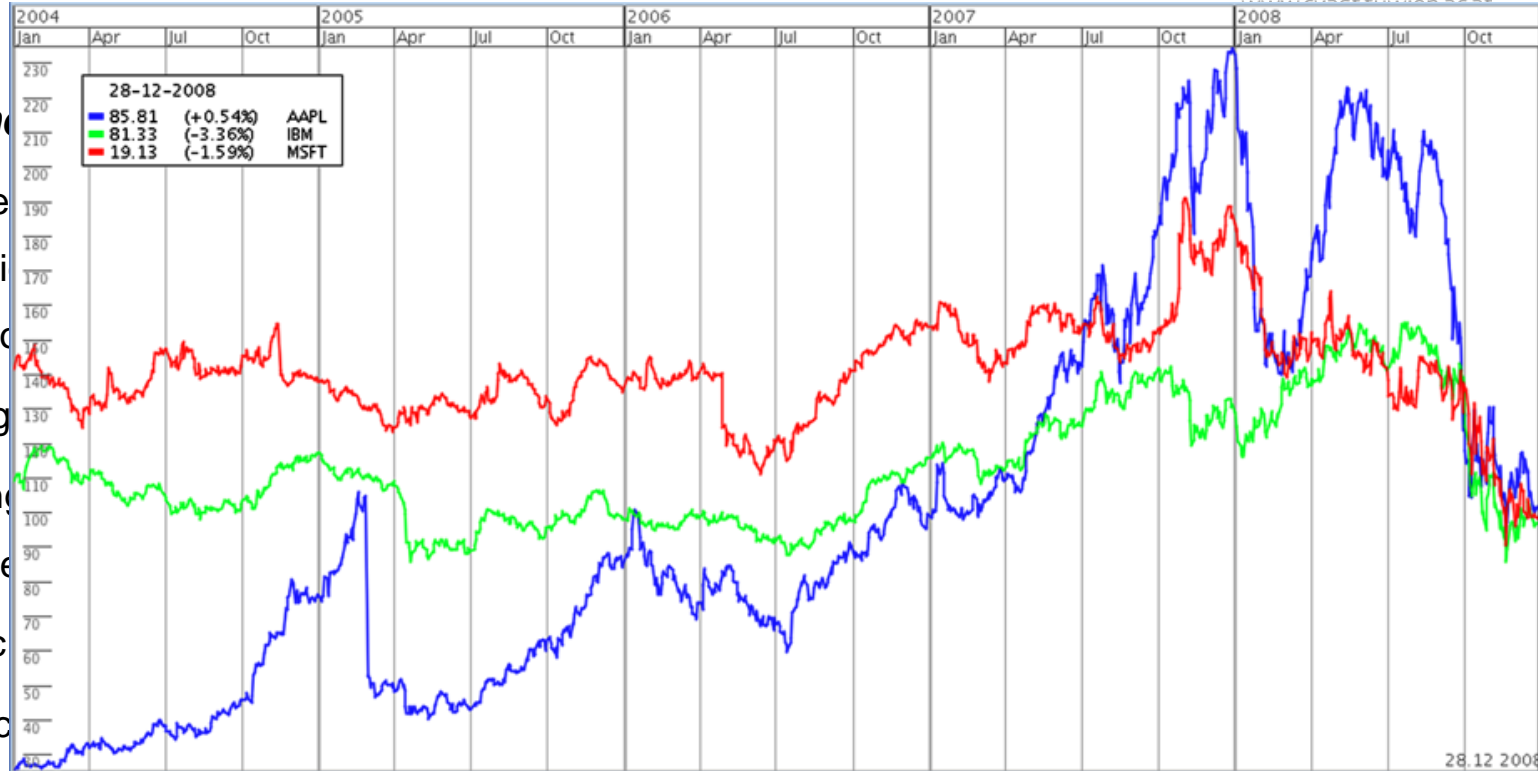




# Visual Mapping of Time

## Dynamic: *Time*

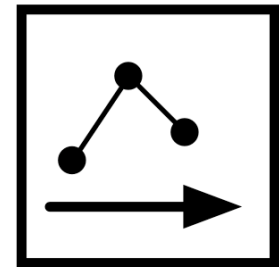
probably the  
no “conversi  
well suited fo  
keeping  
following  
not well suite  
analytic  
no direc




## Static: *Time* → *Space*

mapping of time to visual features


direct comparison of parameters between different points in time is possible




# InfoVis Basics – Marks

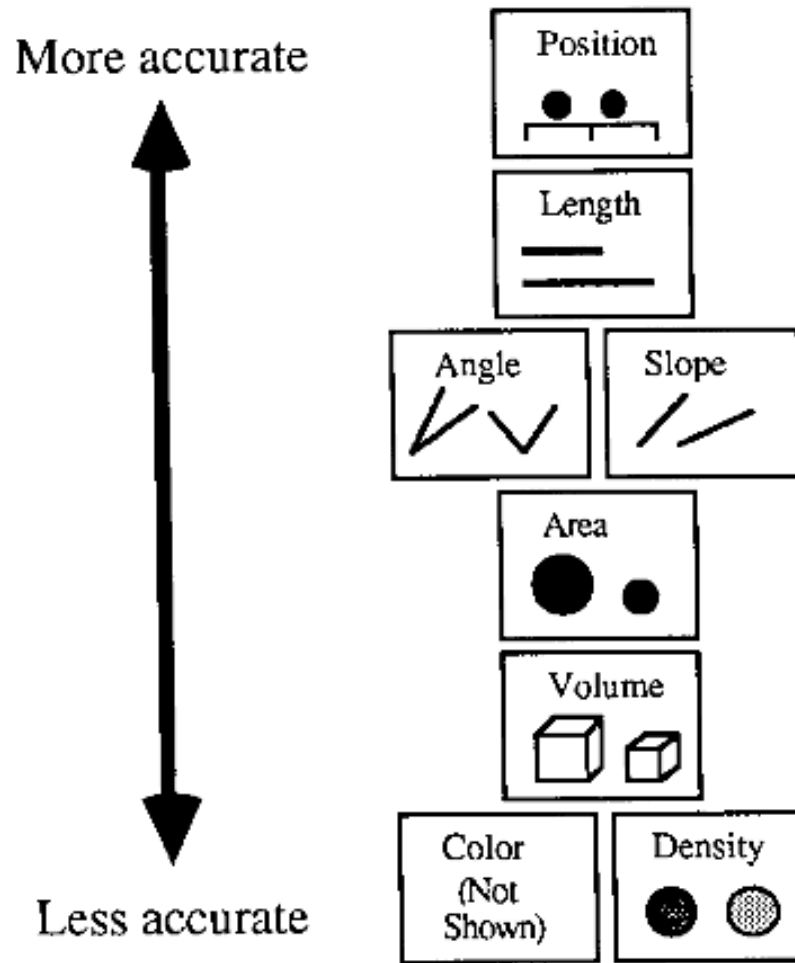
Points (0D) 

Lines (1D) 

Areas (2D) 

Volumes (3D) 

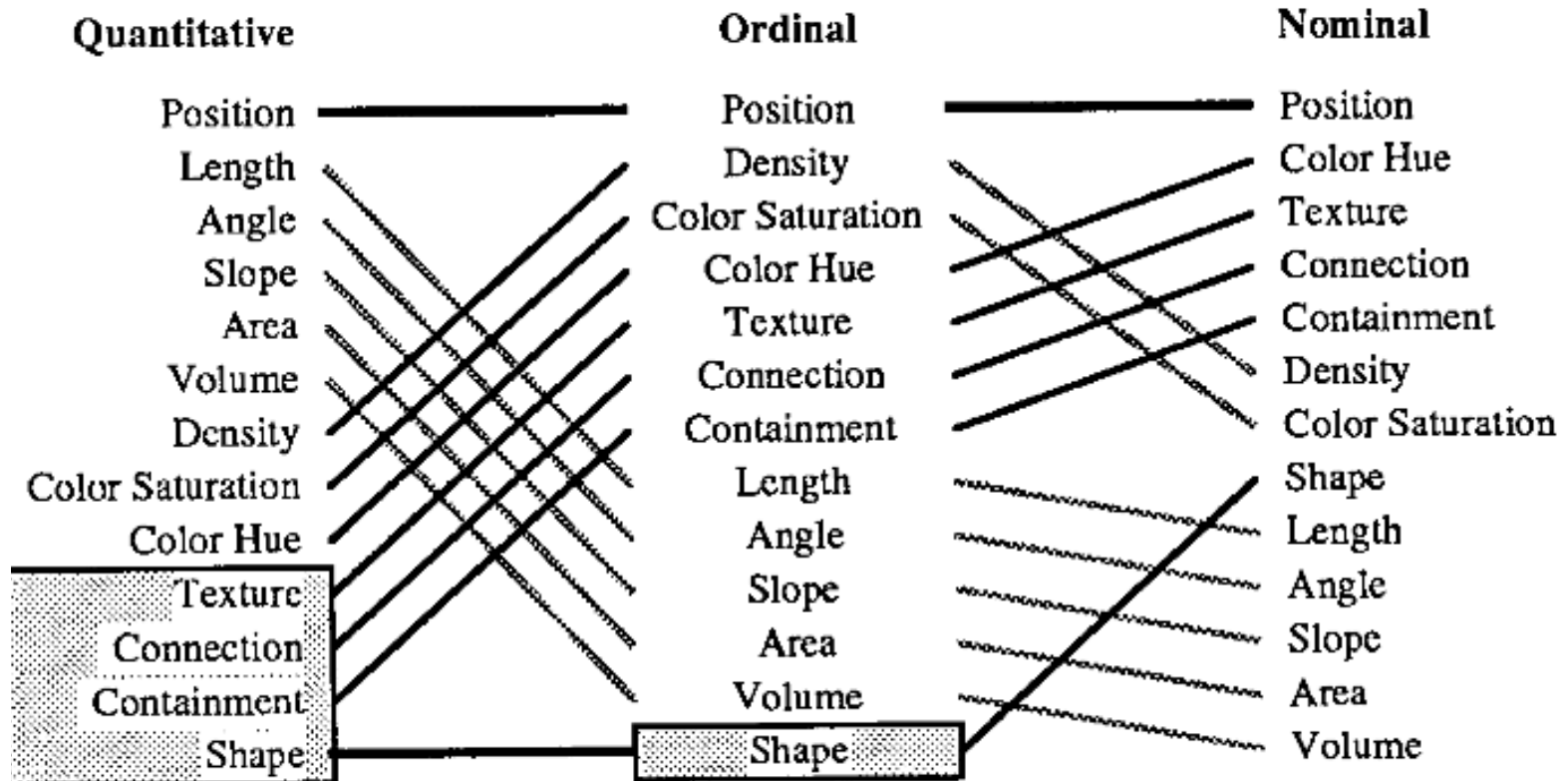
# InfoVis Basics – Visual Variables / Properties of Marks



[Cleveland & McGill, 1984]

# InfoVis Basics – Visual Variables / Properties of Marks

More accurate



Less accurate

[Mackinlay, 1987]

# Visual Variables

## position

most common mapping

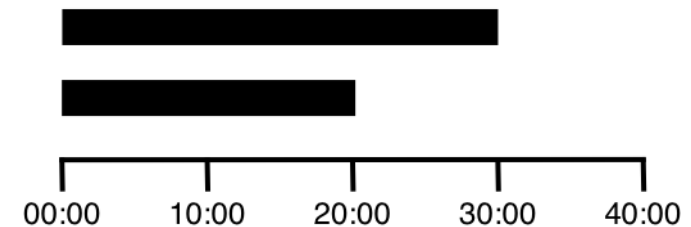
the most accurately perceived visual feature



## length

second most accurate attribute

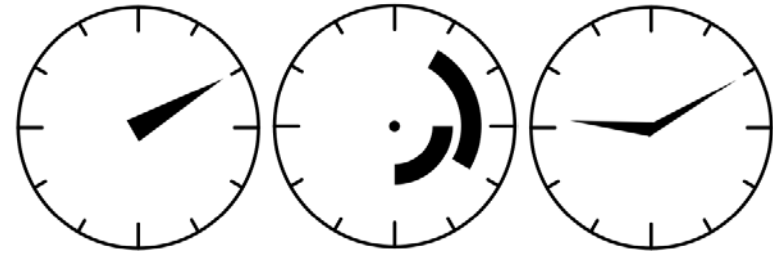
typically, the length of an object denotes the duration, as for example in timelines



# Visual Variables

## angle, slope

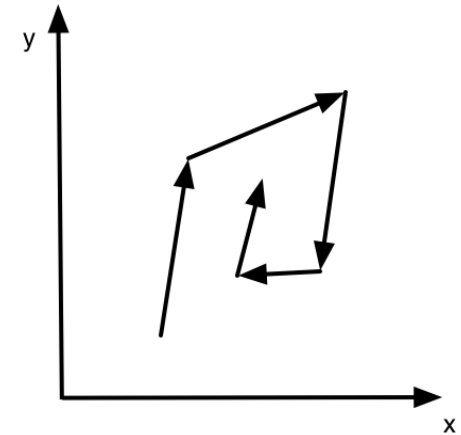
analog-clock-based visualizations



## connection

connecting arrows or lines

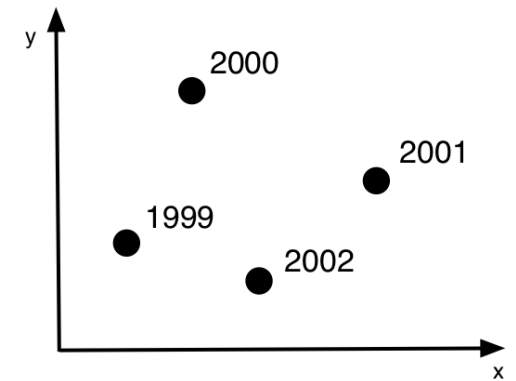
“before element” --> “after element”



## text, label

simple text labelling

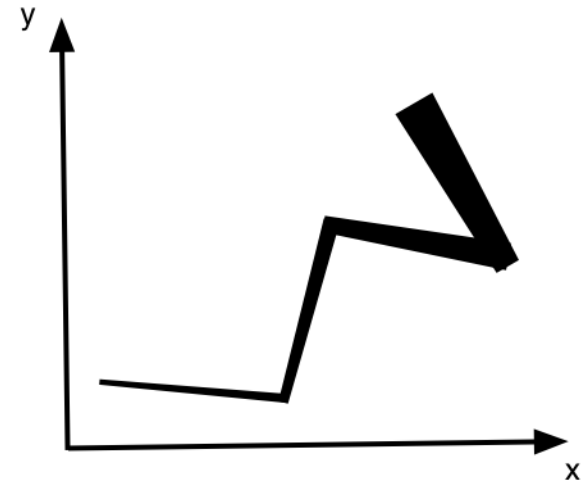
often combined with “connection”



# Visual Variables

## line (thickness)

increasing or decreasing with time

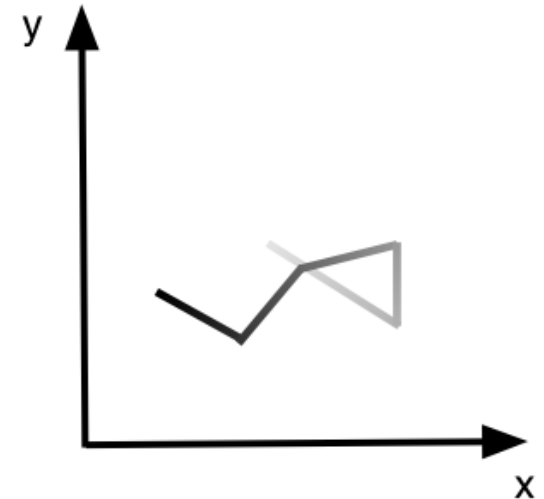


## color (brightness, saturation, hue)

brightness most appropriate

“fading away” against the background

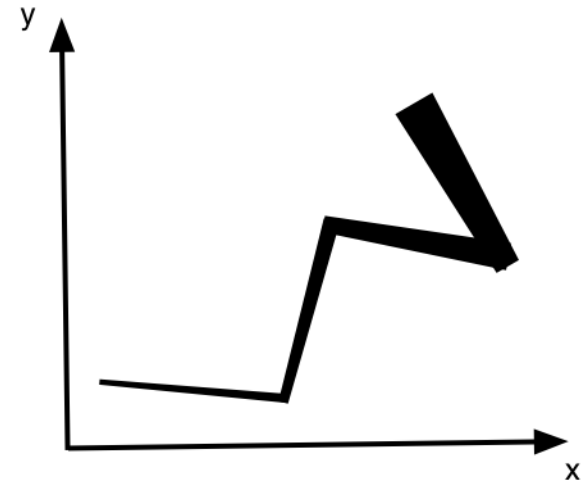
transparency



# Visual Variables

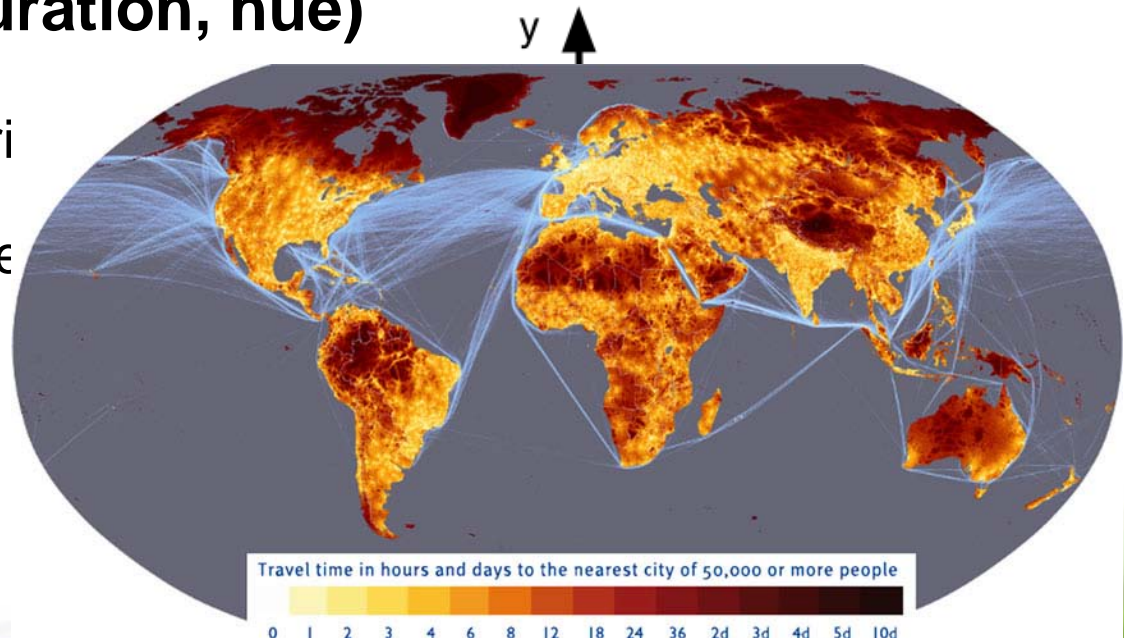
## line (thickness)

increasing or decreasing with time



## color (brightness, saturation, hue)

brightness most appropriate  
“fading away” against the  
transparency





# Visual Variables

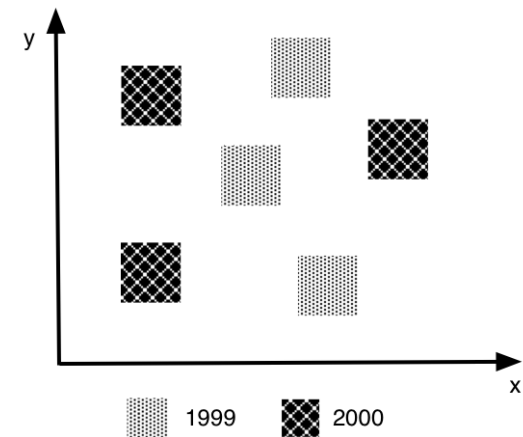
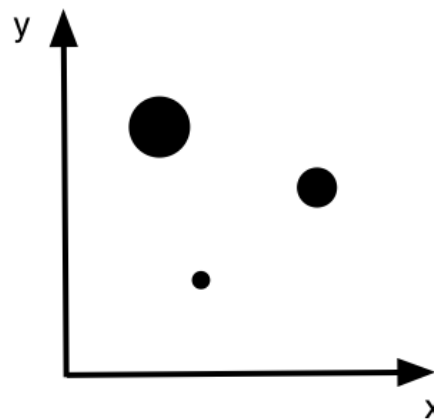
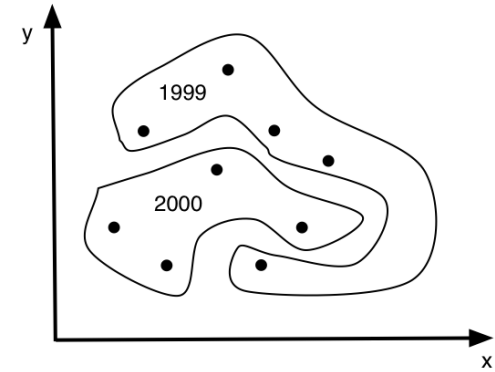
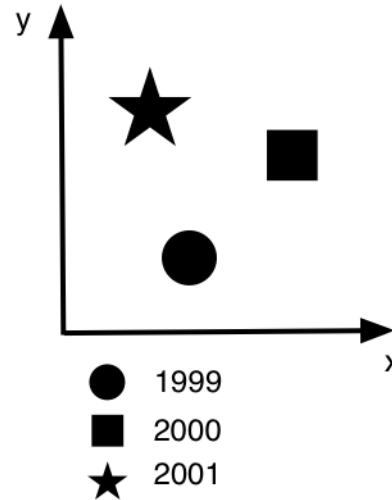
area

enclosure

size

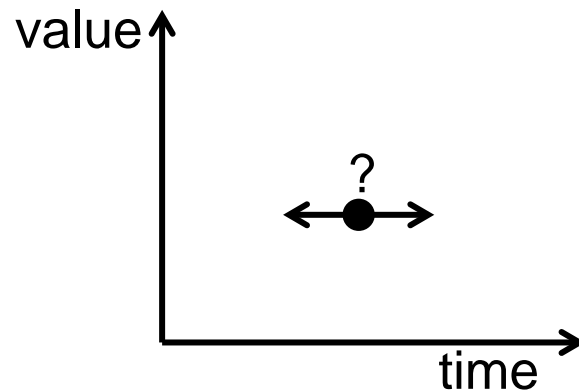
texture

shape



*less suited*





# VISUALIZING TEMPORAL UNCERTAINTY

# Methods to Visually Encode Uncertainty

## Glyphs/Icons:

Error bars, error ellipses, box-plots, confidence intervals,...

Ambiguation,

Orientation of additional lines,

Streamlines, contourlines, isolines,...

## Properties of marks:

Focus (blur),

Opacity (transparency),

Size (length, height, line width,...),

Color (saturation, brightness,...),

Texture,

Animation (blinking, toggle between two views, sequence of possible values...),

Sound,...

## Juxtaposition:

Side-by-side displays of competing results,

Side-by-side displays of data values and uncertainty values,...

Additional transparent layers,

Additional symbols,...

*[Pang et al., 1997]*

*[Olston and Mackinlay, 2002]*

*[Correa et al., 2009]*

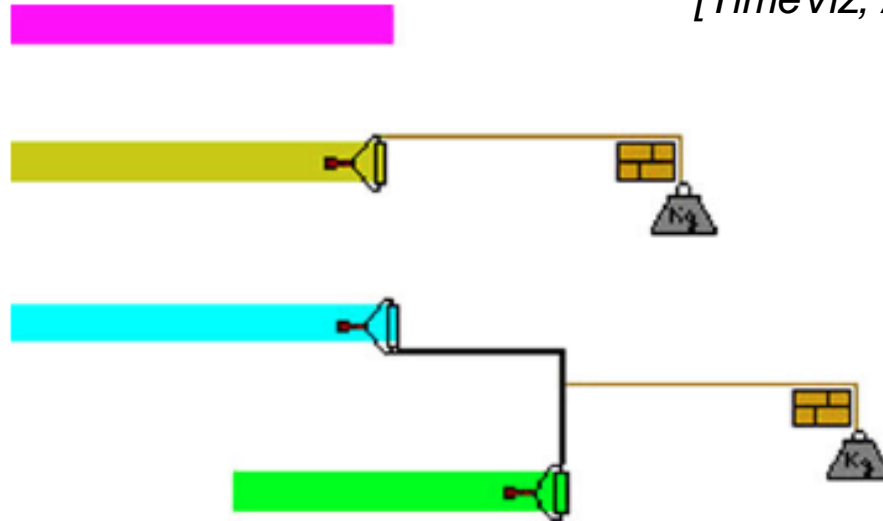
*[Senaratne and Gerharz, 2011]*

*[Kandel et al., 2011]*

*[Brodie et al., 2012]*

# Paint Strips

[Chittaro and Combi, 2003]  
[TimeViz, Aigner, et al., 2011]



**Fig. 7.20:** Paint strips indicate the location and duration of time intervals, effectively allowing users to assess relationships of intervals. Temporal indeterminacy of intervals is indicated by paint rollers that can move flexibly within certain constraints, which are represented by wall elements.

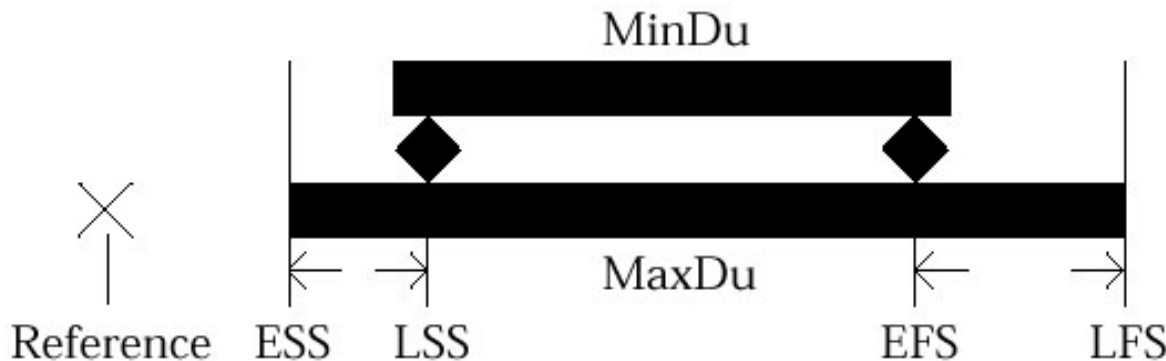
*Source: Image courtesy of Luca Chittaro.*

# Time Annotation Glyph

[Kosara and Miksch, 1999]

Definition:

[[ESS, LSS], [EFS, LFS], [MinDu, MaxDu], Reference]



For representation of future planning data (uncertainty / indeterminacy)

Characteristics:

Time points are relative (Reference point)

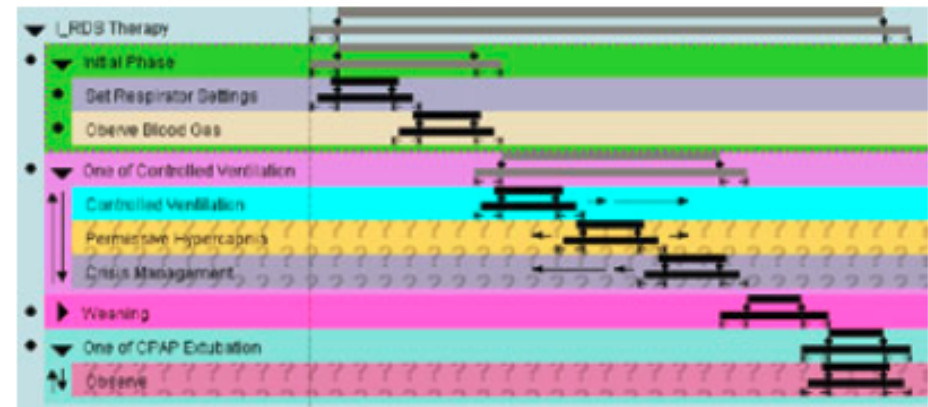
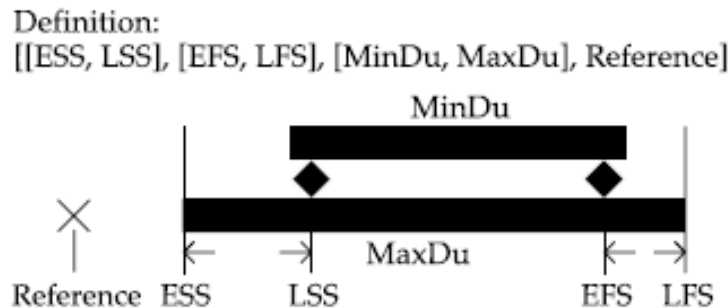
ESS/EFS: earliest starting/finishing shift

LSS/LFS: latest starting/finishing shift

MinDu/MaxDu: Minimum/Maximum duration

# Time Annotation Glyph

[Kosara and Miksch, 2001]  
[TimeViz, Aigner, et al., 2011]

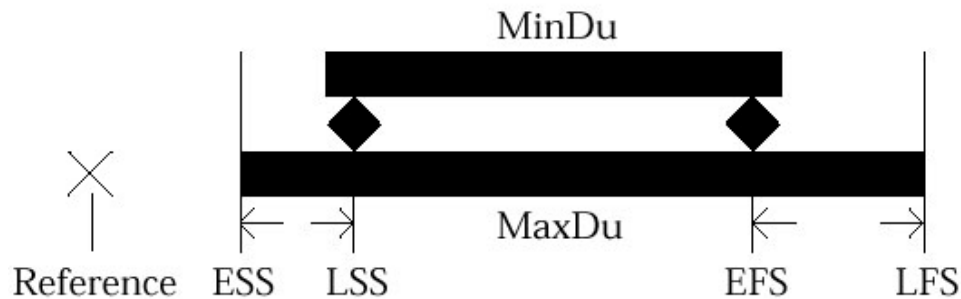


**Fig. 7.22:** The time annotation glyph was designed to represent the temporal constraints of medical treatment plans. It uses the metaphor of bars that lie on pillars. Left: Single glyph and associated parameters. Right: Usage in a tool for representing the temporal and hierarchical aspects of a medical treatment plan as well as the execution order of individual parts.

*Source: Images courtesy of Robert Kosara.*

# Time Annotation Glyph 2/2

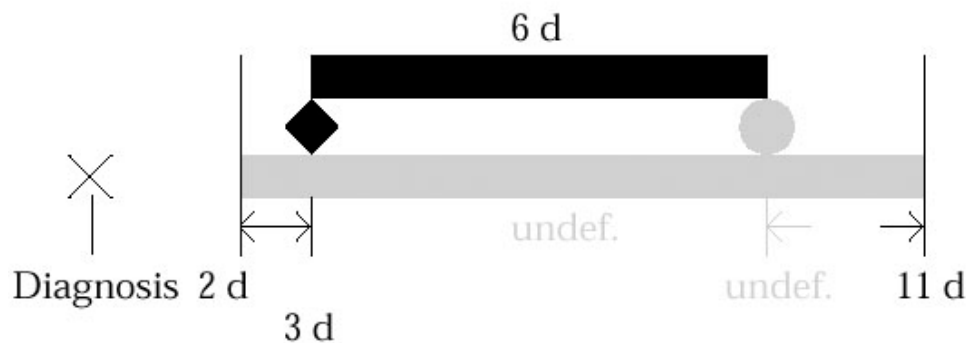
Definition:  
[[ESS, LSS], [EFS, LFS], [MinDu, MaxDu], Reference]



MinDu and LFS defined to higher precision than time axis



Example: [[2 d, 3 d], [\_, 11 d], [6 d, \_], Diagnosis]



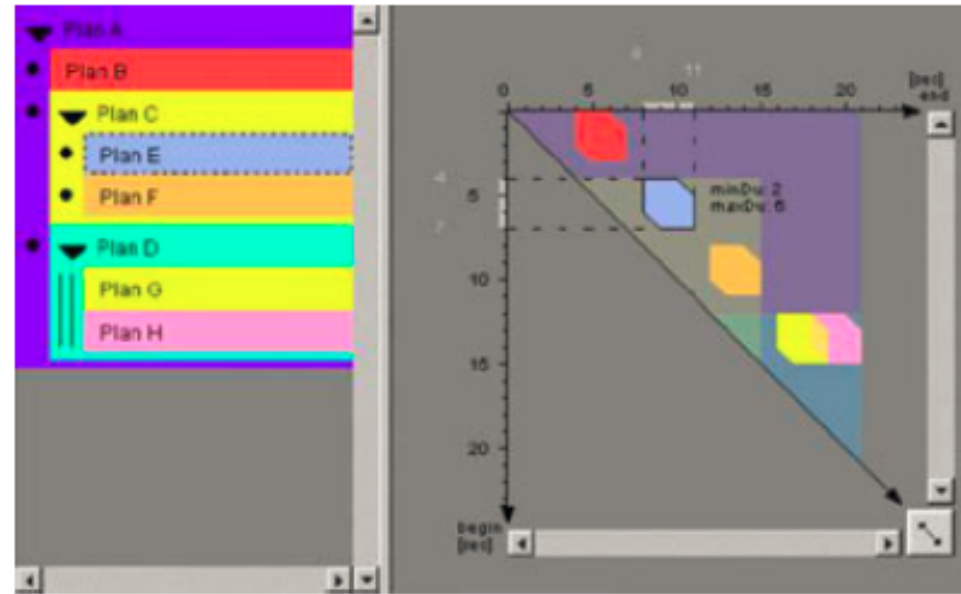
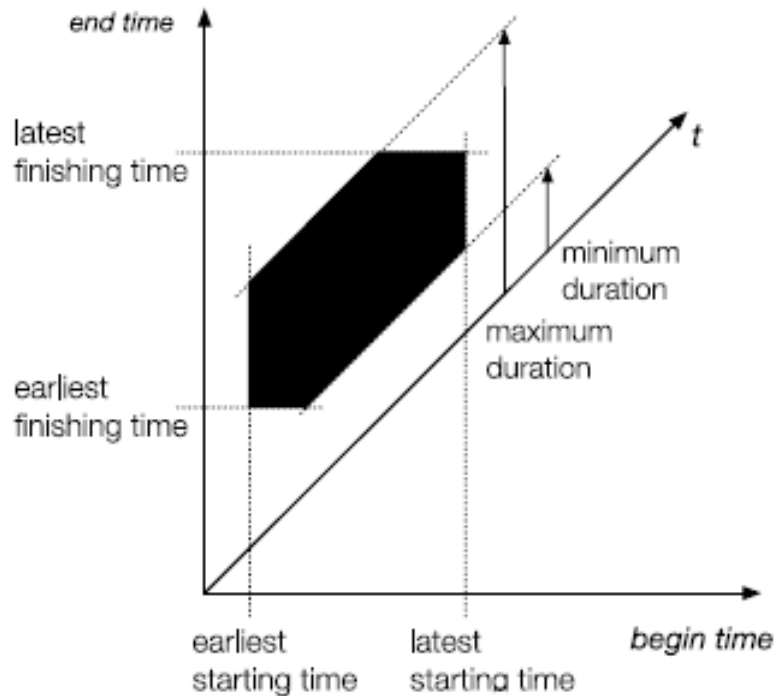
MinDu and LFS defined to lower precision than time axis



# SOPO Diagram

[Kosara and Miksch, 2002]

[TimeViz, Aigner, et al., 2011]



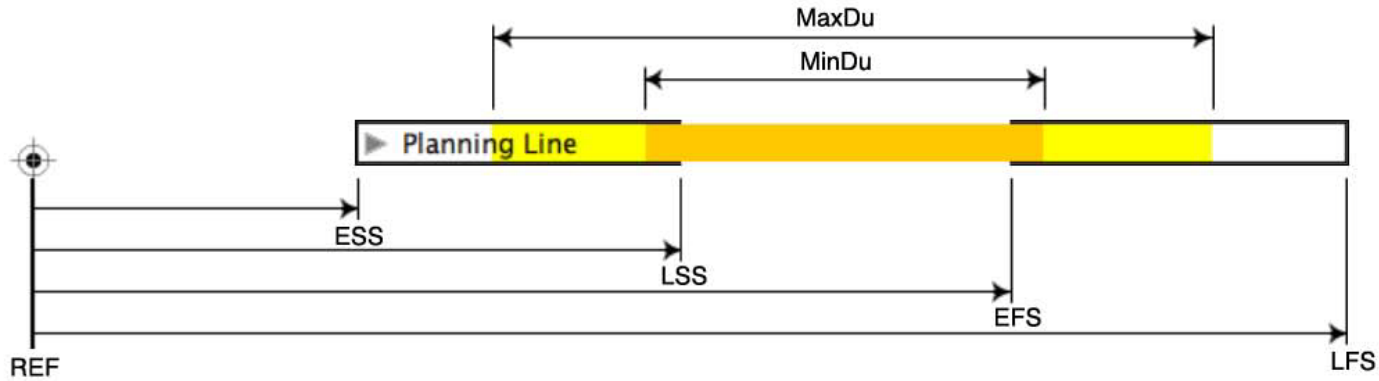
**Fig. 7.23:** A SOPO diagram shows the possible configurations of the begin and end times of an event via a constrained polygonal shape. Right: SOPOView – an interactive visualization tool for working with SOPOs applied for medical treatment plans.

*Source: Images courtesy of Robert Kosara.*



# PlanningLines

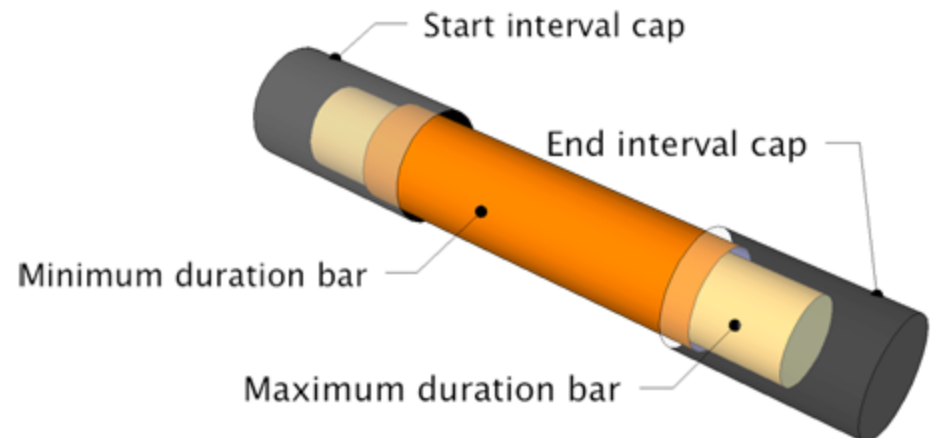
[Aigner et al., 2005]



REF...Reference Point

MinDu...Minimum Duration  
MaxDu...Maximum Duration

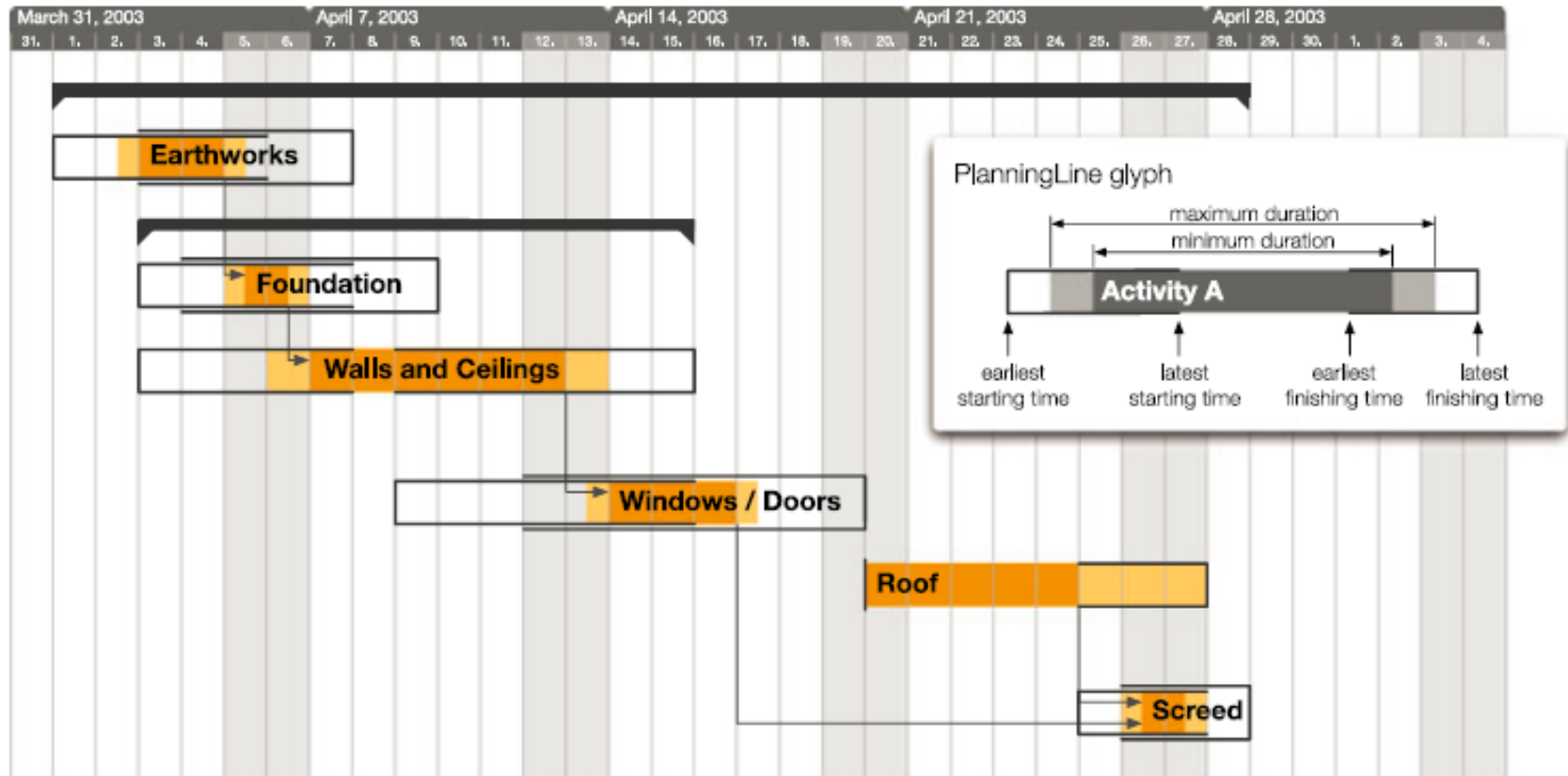
ESS...Earliest Starting Shift  
LSS...Latest Starting Shift  
EFS...Earliest Finishing Shift  
LFS...Latest Finishing Shift



# PlanningLines

[Aigner et al., 2005]

[TimeViz, Aigner, et al., 2011]



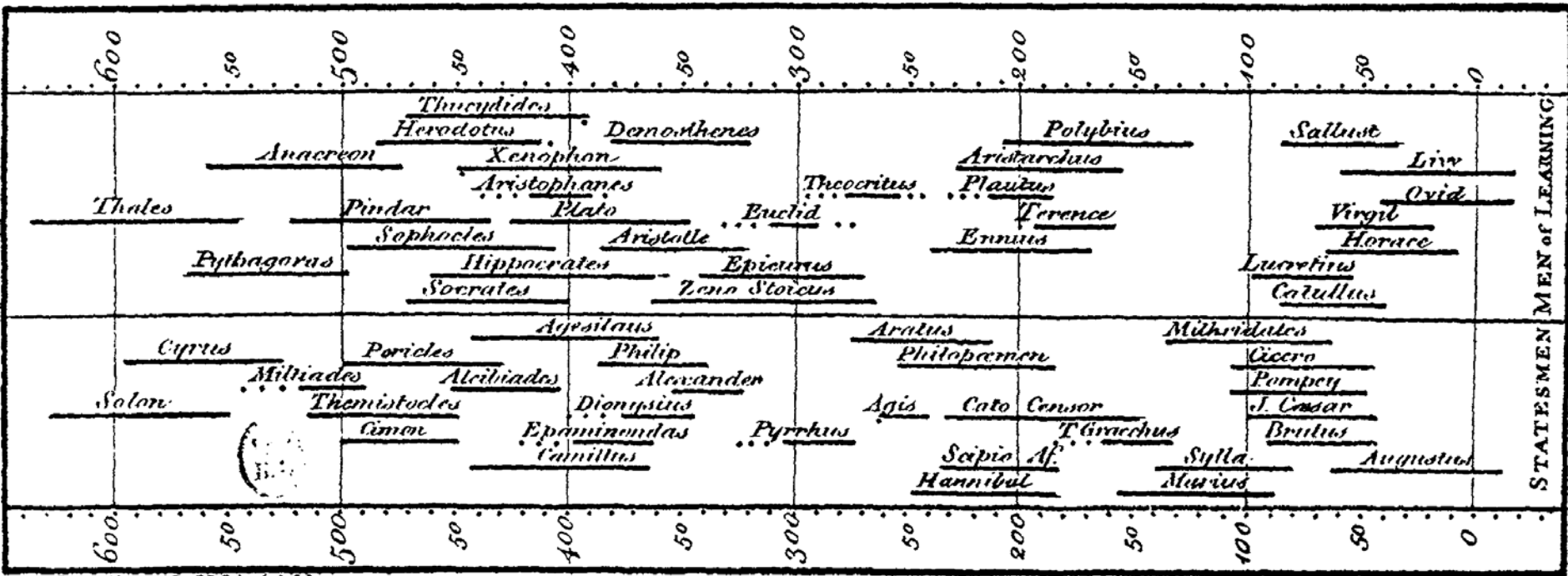
**Fig. 7.21:** Project plan of construction works that represents temporal uncertainties via PlanningLines. A PlanningLine glyph consists of two encapsulated bars, which represent minimum and maximum duration. The bars are bounded by two caps encoding the start and end intervals.  
*Source: Adapted from Aigner et al. (2005).*

# Joseph Priestley's chart of biography

[Priestley, 1765]

[TimeViz, Aigner, et al., 2011]

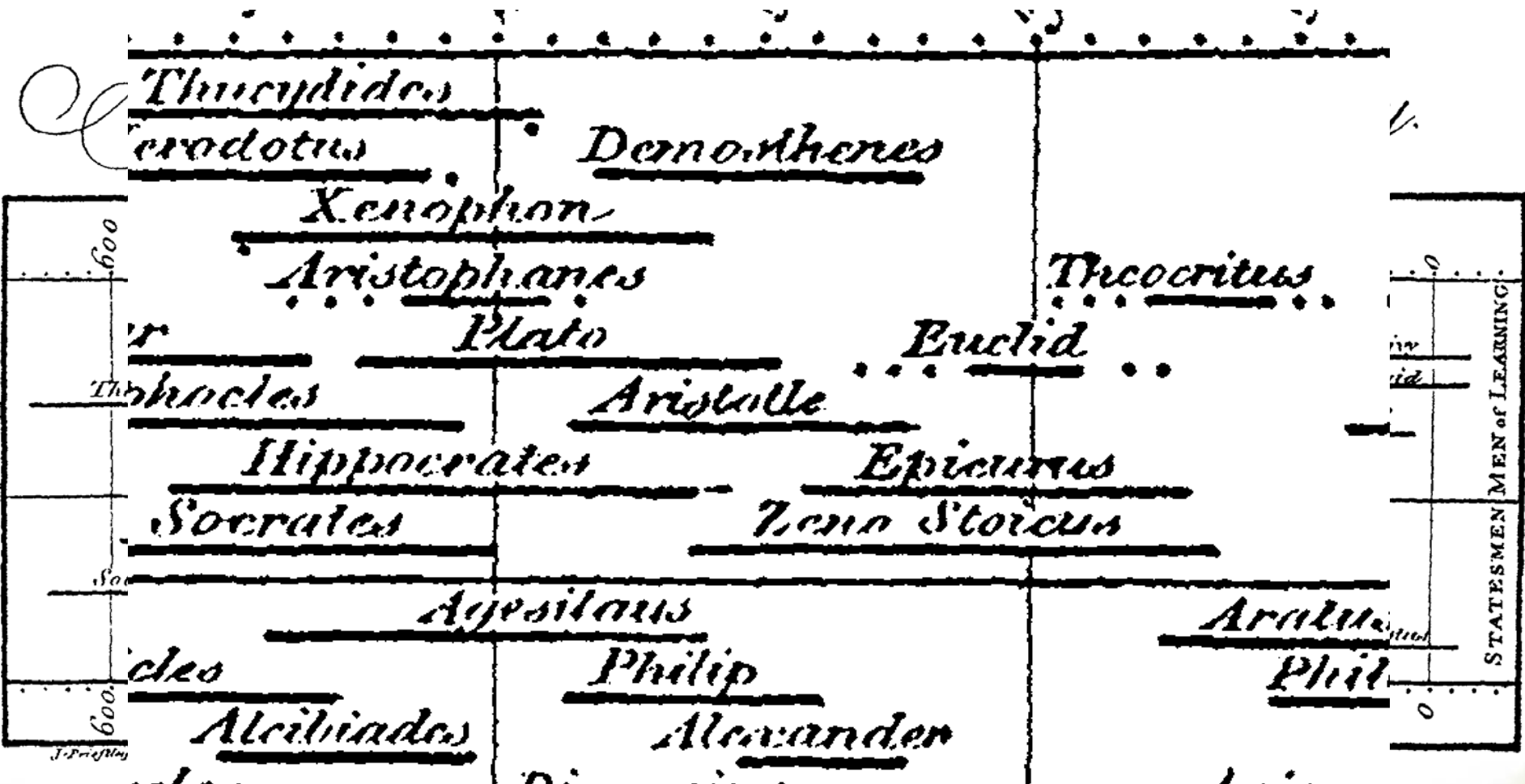
## A Specimens of a Chart of Biography.



# Joseph Priestley's chart of biography

[Priestley, 1765]

[TimeViz, Aigner, et al., 2011]



# Methods to Visually Encode Uncertainty

## Glyphs:

Error bars, error ellipses, box-plots, confidence intervals,...

Ambiguation,

Orientation of additional lines,

Streamlines, contourlines, isolines,...

## Properties of marks:

Focus (blur),

Opacity (transparency),

Size (length, height, line width,...),

Color (saturation, brightness,...),

Texture,

Animation (blinking, toggle between two views, sequence of possible values...),

Sound,...

## Juxtaposition:

Side-by-side displays of competing results,

Side-by-side displays of data values and uncertainty values,...

Additional transparent layers,

Additional symbols,...

*... often used to encode  
temporal uncertainty*

[Pang et al., 1997]

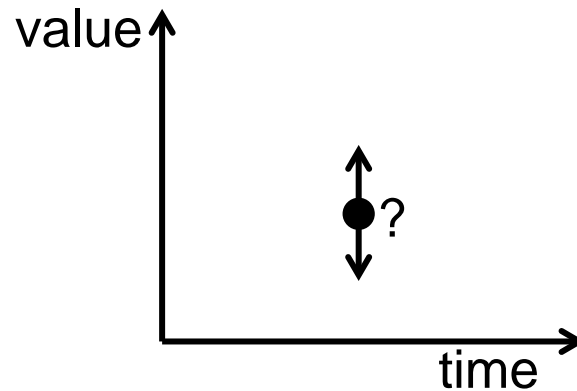
[Olston and Mackinlay, 2002]

[Correa et al., 2009]

[Senaratne and Gerharz, 2011]

[Kandel et al., 2011]

[Brodie et al., 2012]



# VISUALIZING UNCERTAINTY OF TIME-ORIENTED DATA

# What is Time-Oriented Data?

No formal definition

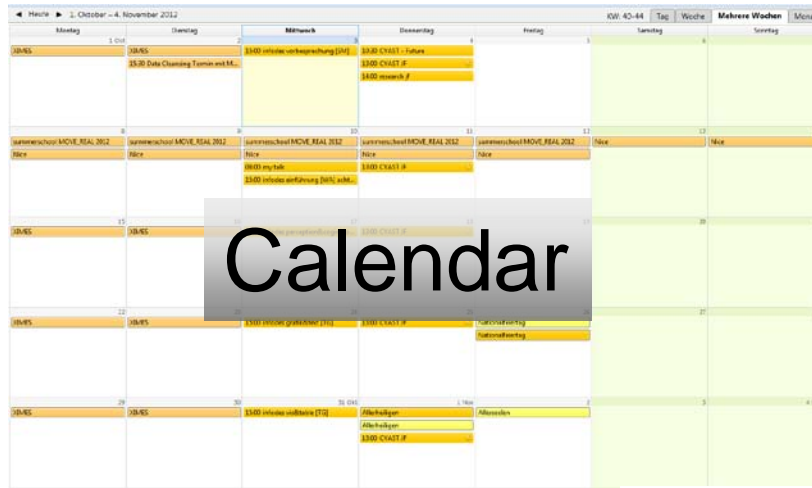
What is considered as time-oriented data depends on the intended **task**

*A possible definition:*

Data, where **changes over time**  
or **temporal aspects** play a  
central role or are of interest.



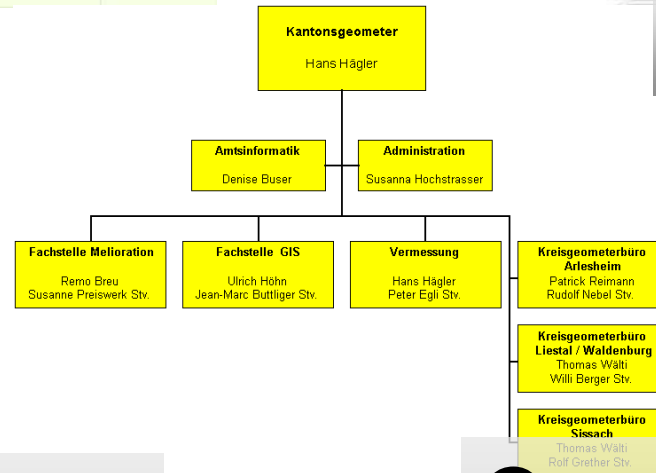
# Time-Oriented Data?



iPad price



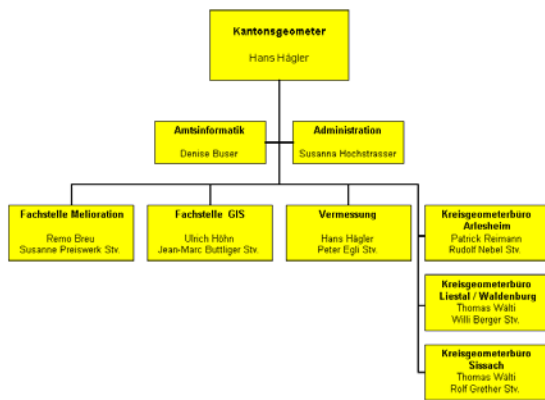
Snow height & sunshine hours



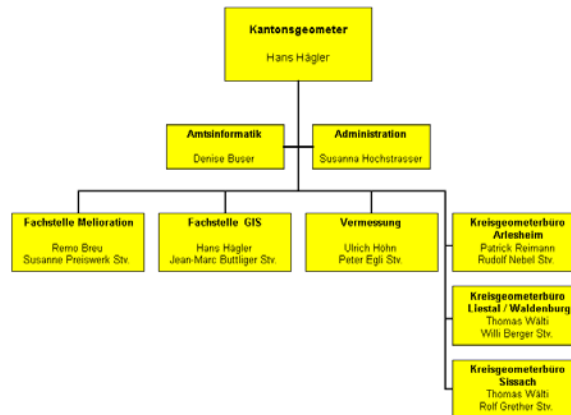
Organization chart



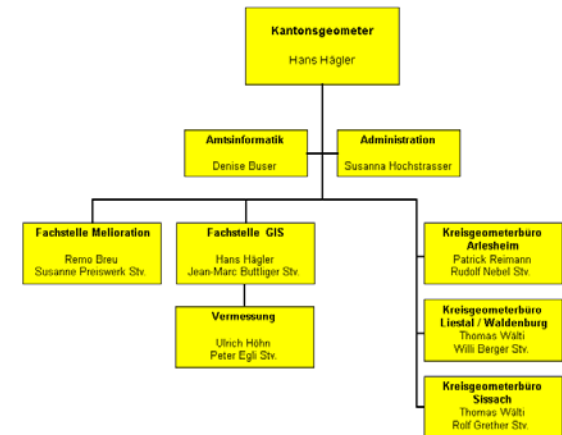
# Organization Chart



1998



2000



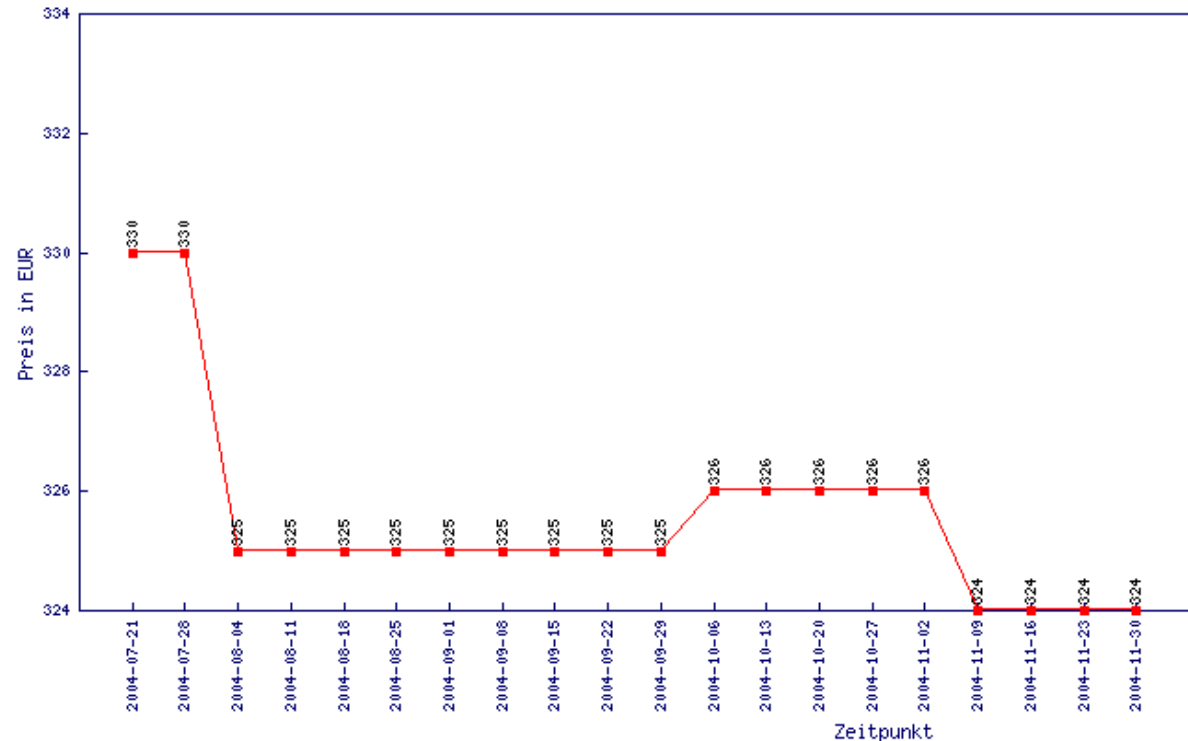
2002

time

# iPod Price





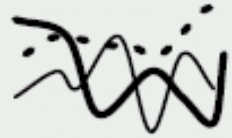


Preis in €	Anbieter	Händler-Bewertung	Verfügbarkeit lt. Händler
			Versand
<b>324,--</b> 	T-Online-Shop <a href="#">[zum Shop]</a>	 Note: 2,24	Versandfertig in ca. 14 Tagen



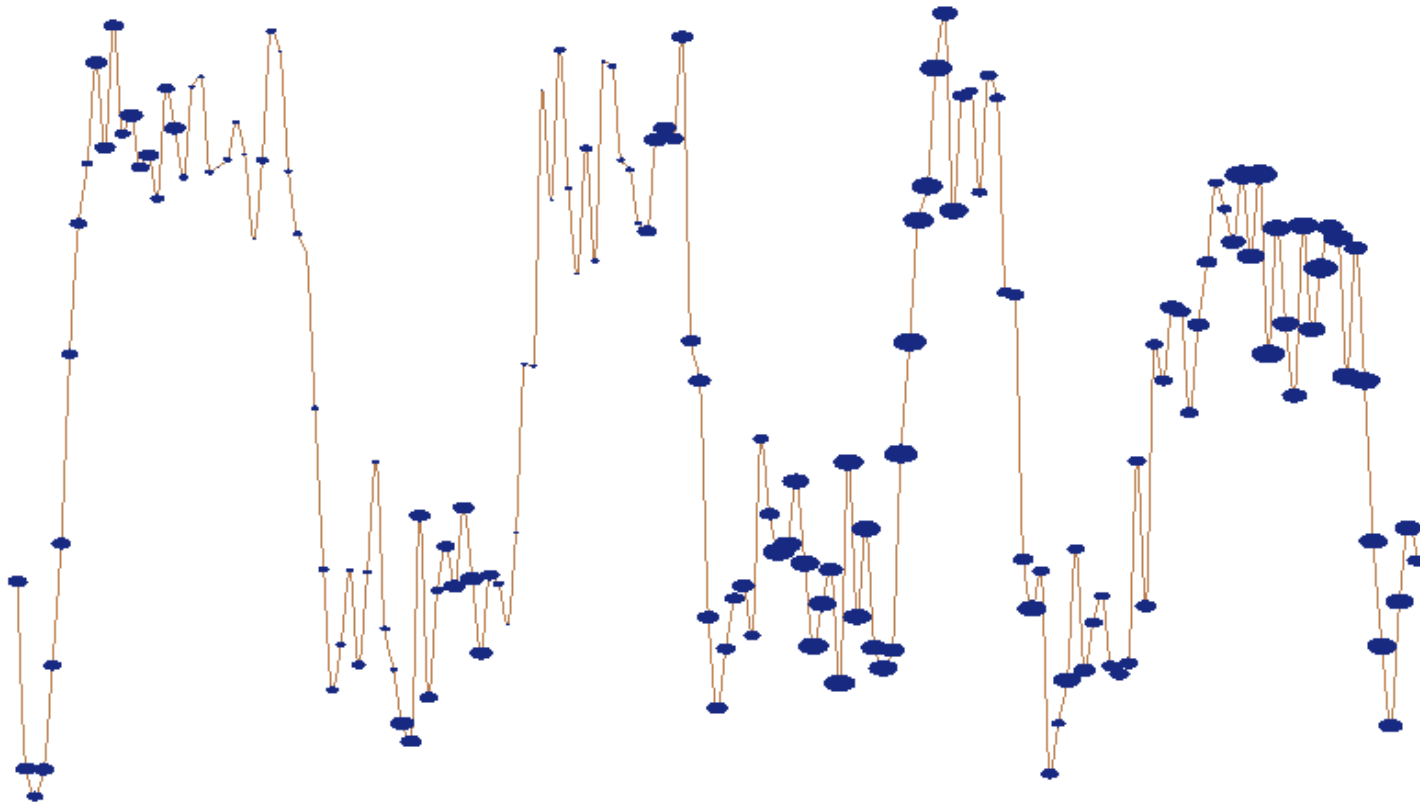
<a href="#">Infos</a> <a href="#">AGB</a> <a href="#">Meinungen</a>	Note: 1,09 14 Bewertungen	<b>Details zur Anfrage</b> Vorkasse: € 5,30 Nachnahme: zzgl. € 4,80 kostenlose Zustellung in
---	------------------------------	---

# Characterizing Data

scale	3.14 3.27 4.88 quantitative	coconut banana apple qualitative
frame of reference	▼ abstract	 spatial
kind of data	 events	 states
number of variables	 univariate	 multivariate

# Quantitative Time-Oriented Data

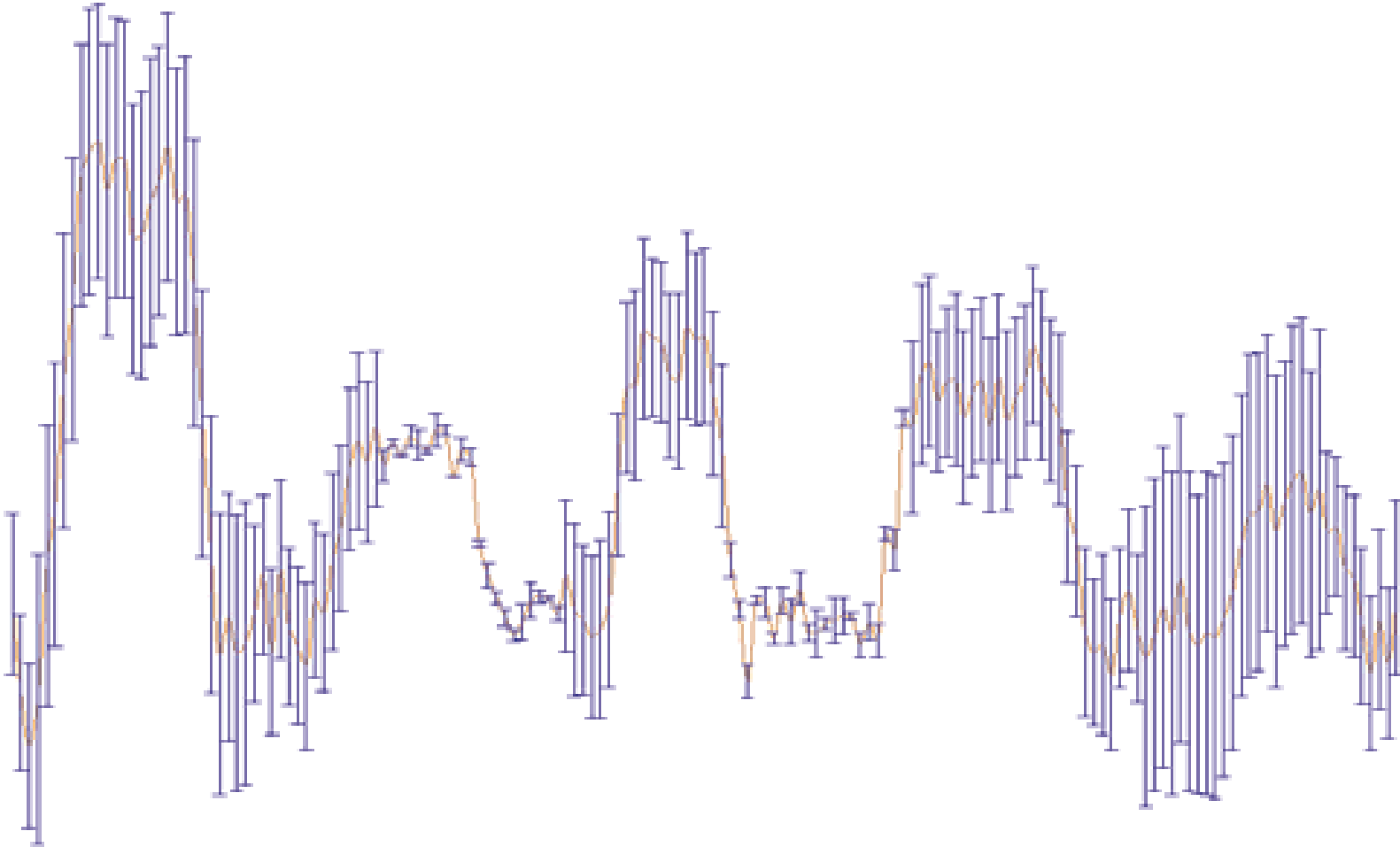
size of marks



*[Sanyal et al., 2009]*

# Quantitative Time-Oriented Data

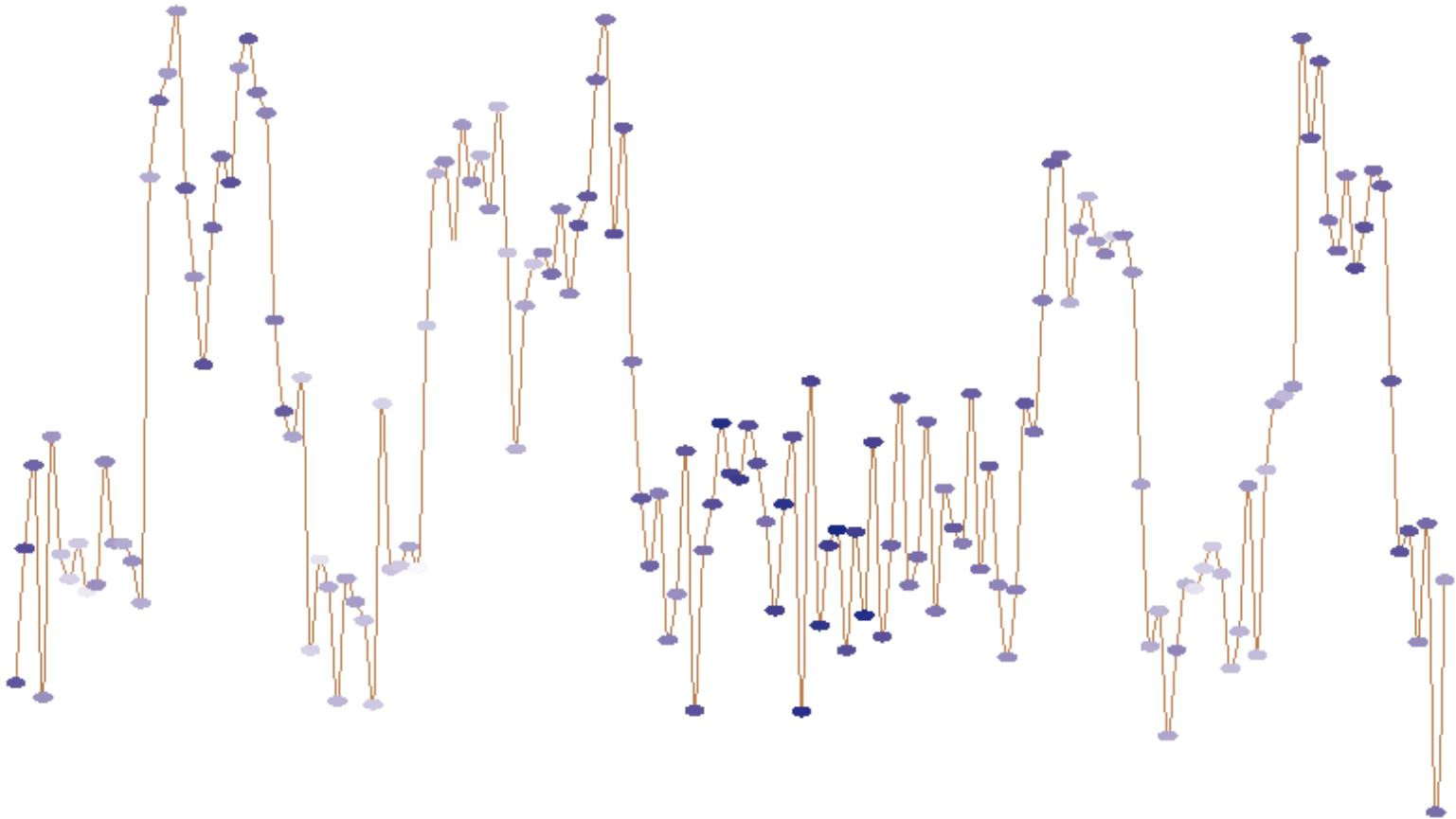
error bars



*[Sanyal et al., 2009]*

# Quantitative Time-Oriented Data

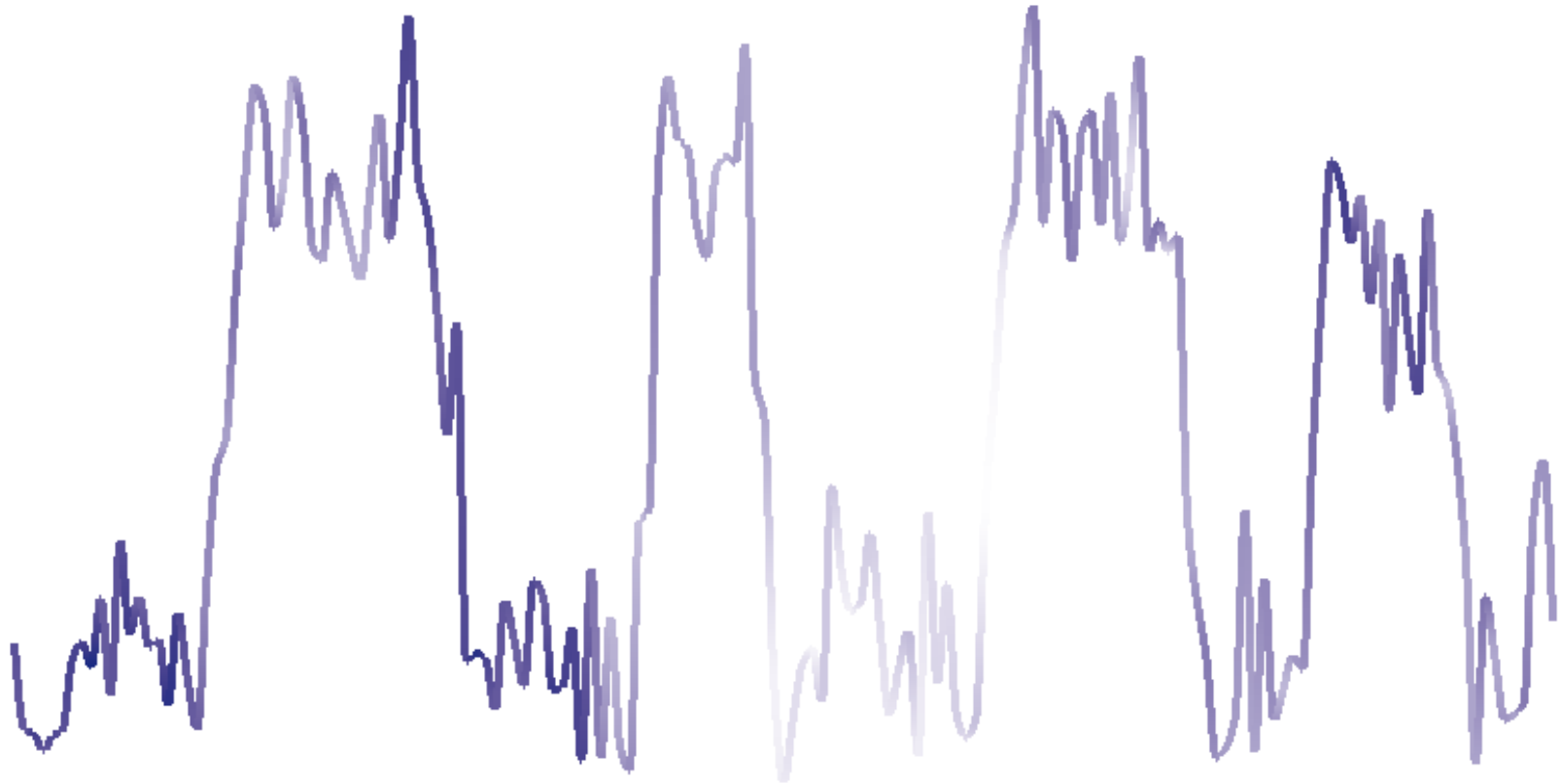
color of marks



[Sanyal et al., 2009]

# Quantitative Time-Oriented Data

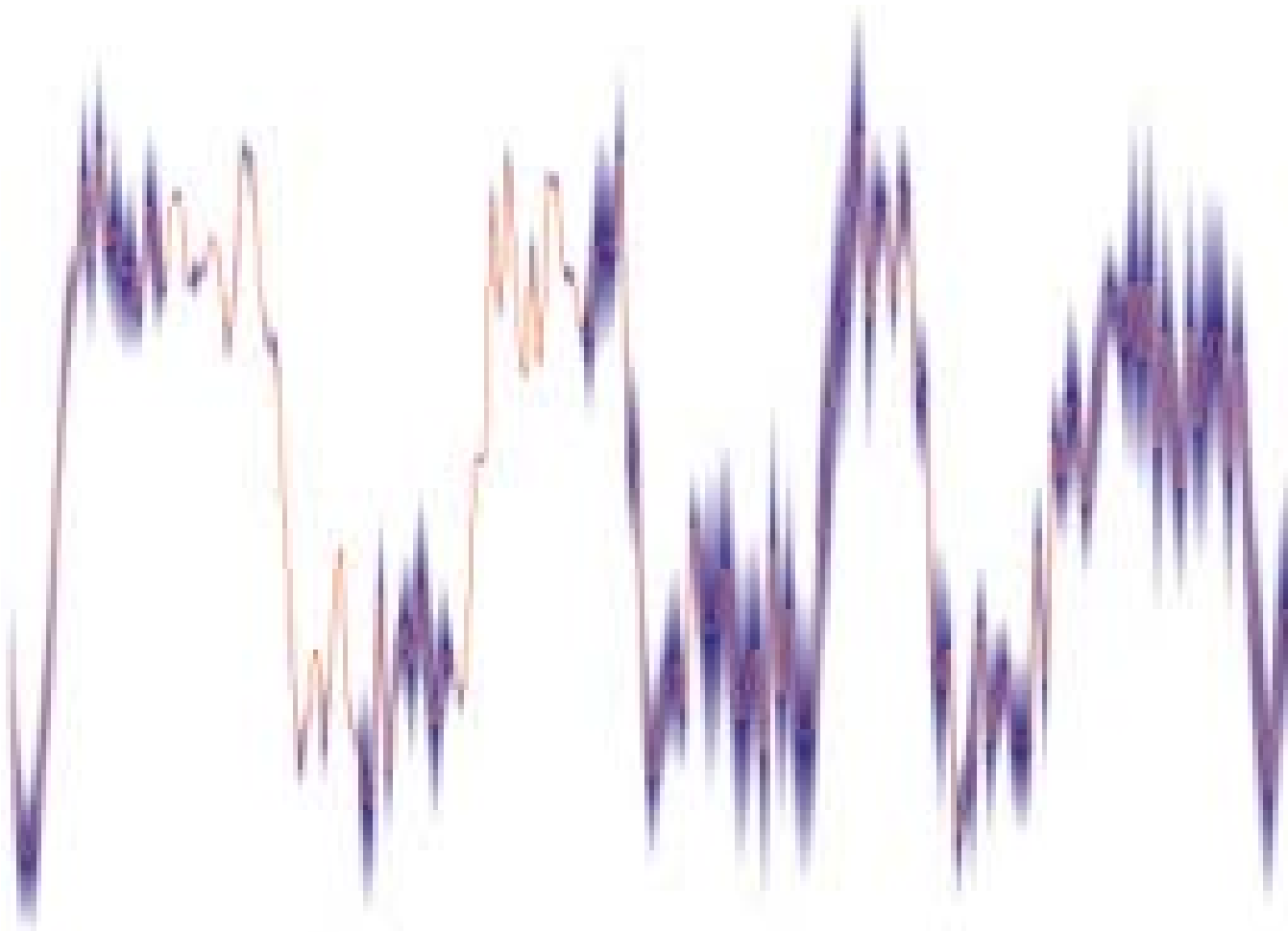
color of line



*[Sanyal et al., 2009]*

# Quantitative Time-Oriented Data

width of gradient

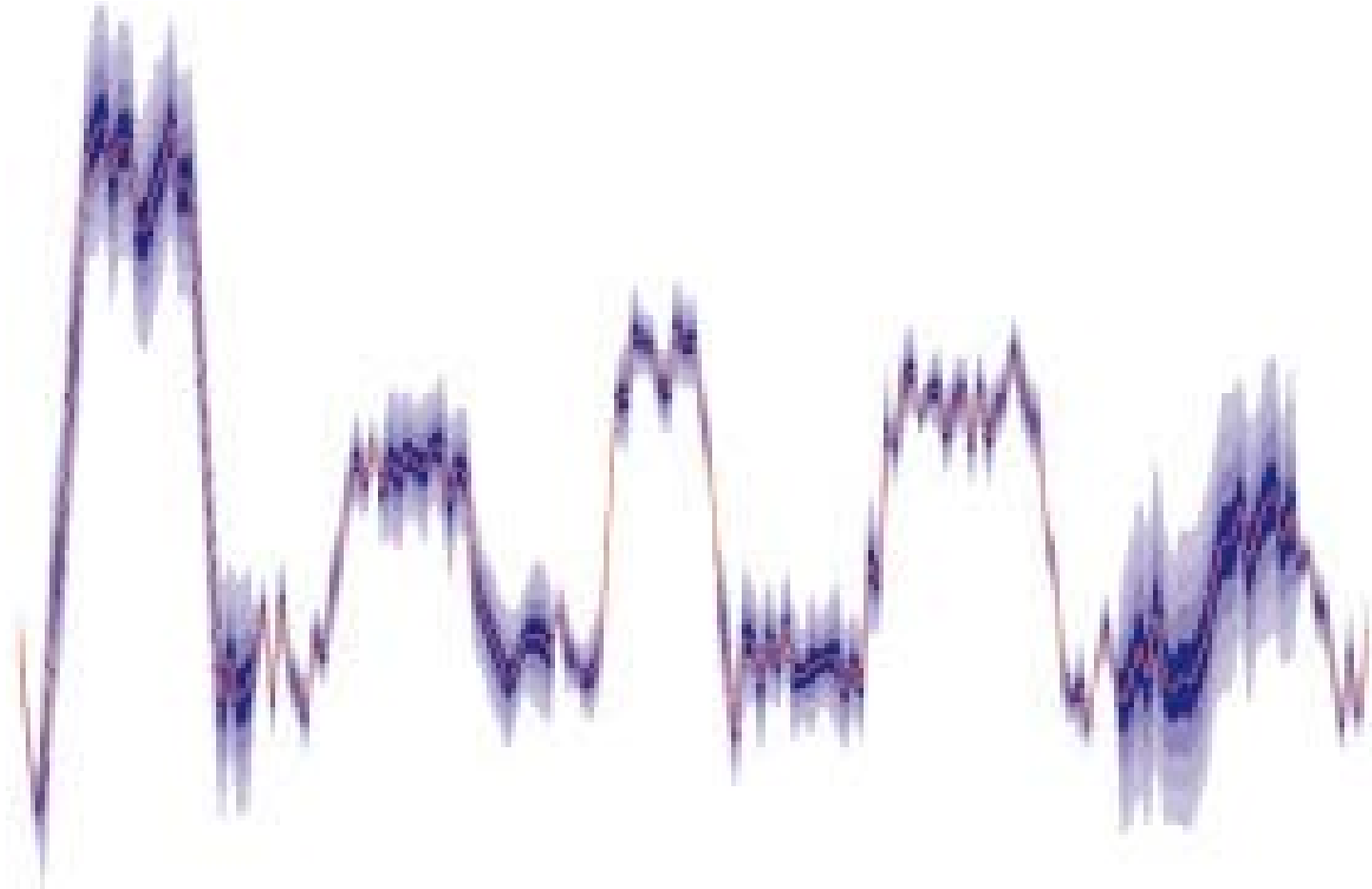


*[Sanyal et al., 2009]*



# Quantitative Time-Oriented Data

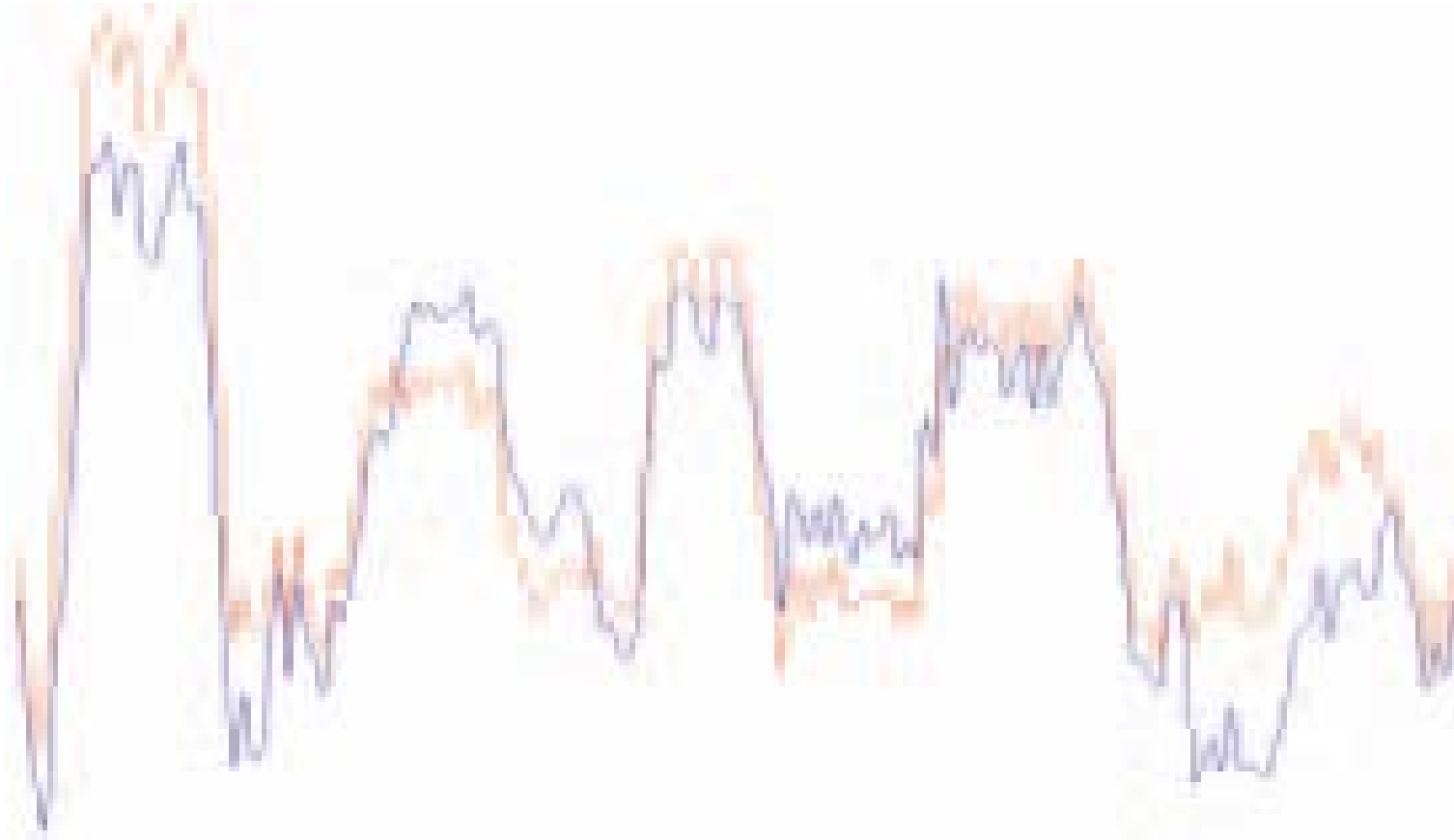
width of striped gradient



*[Sanyal et al., 2009]*

# Quantitative Time-Oriented Data

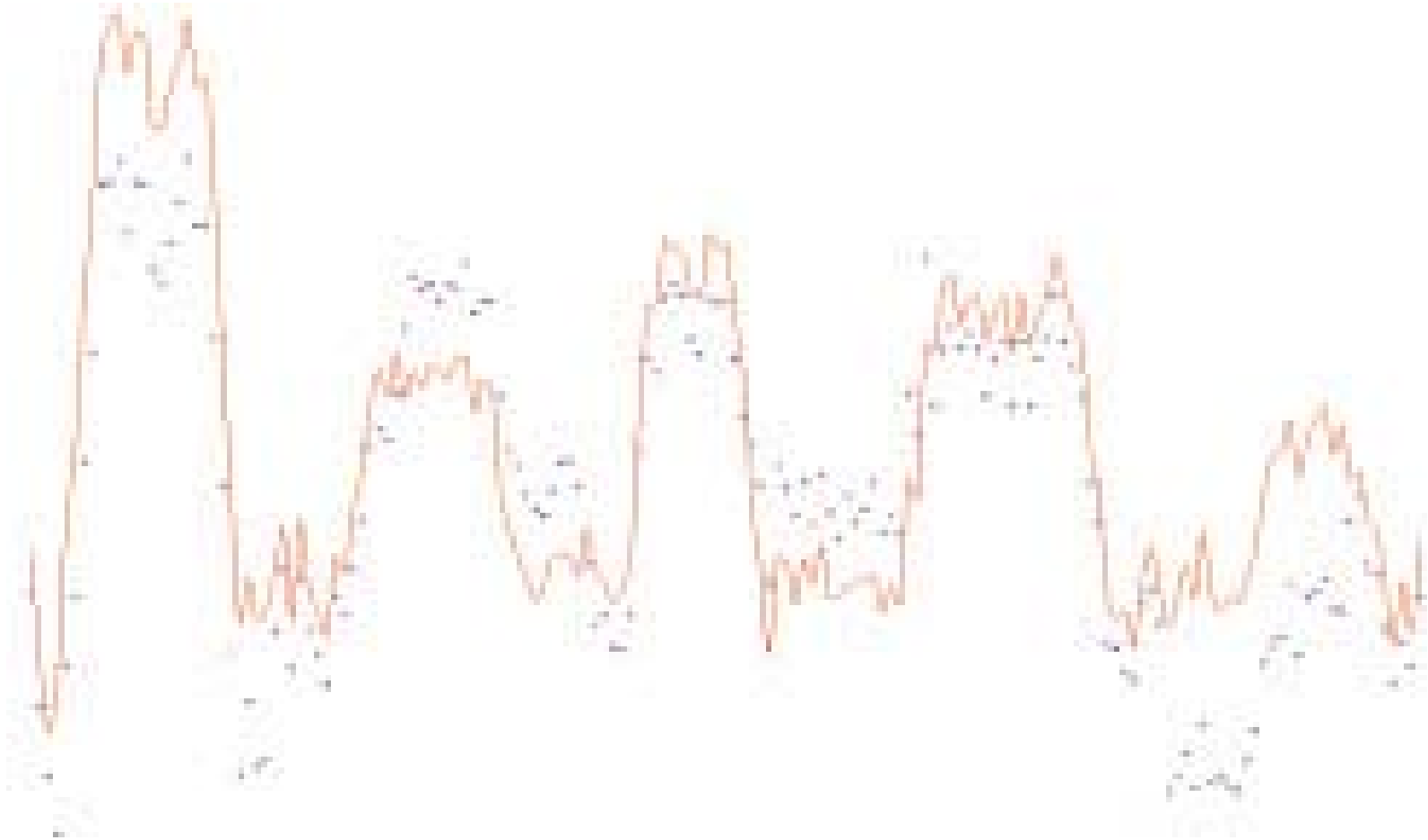
animation of additional line



*[Sanyal et al., 2009]*

# Quantitative Time-Oriented Data

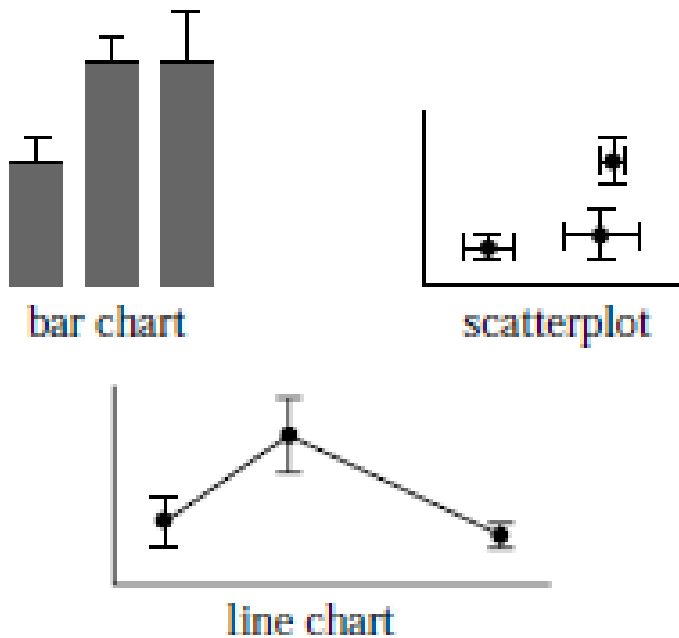
animation of additional marks



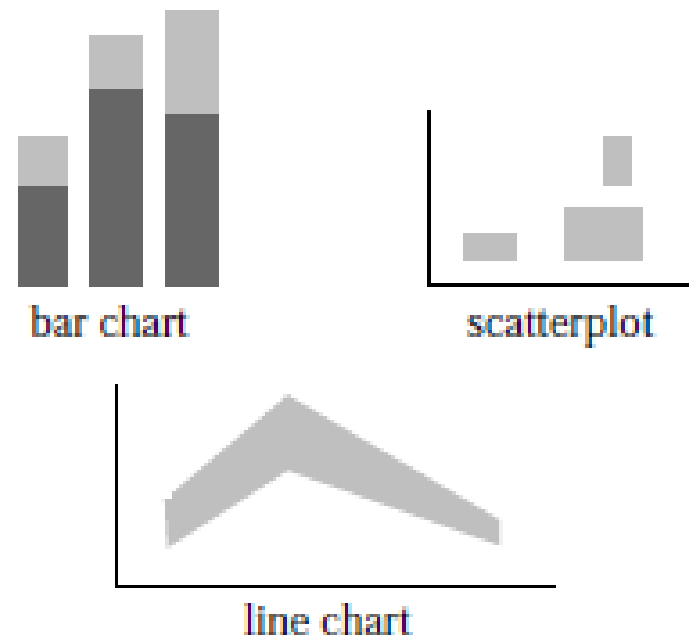
*[Sanyal et al., 2009]*

# Statistical vs. Bounded Uncertainty

error bars

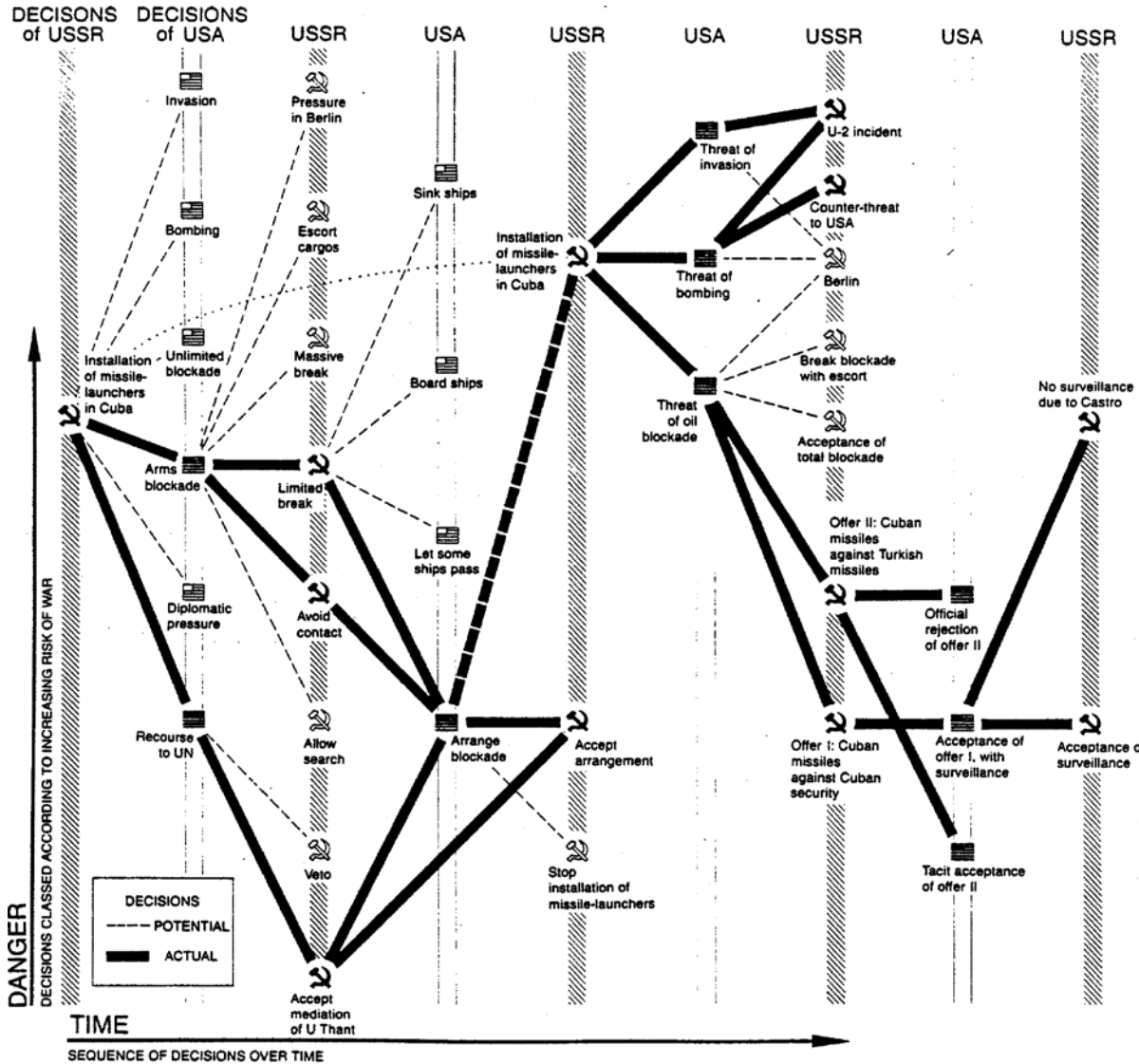


ambiguation



[Olston and Mackinlay, 2002]

# Qualitative T-O Data : Cuban Missile Crisis

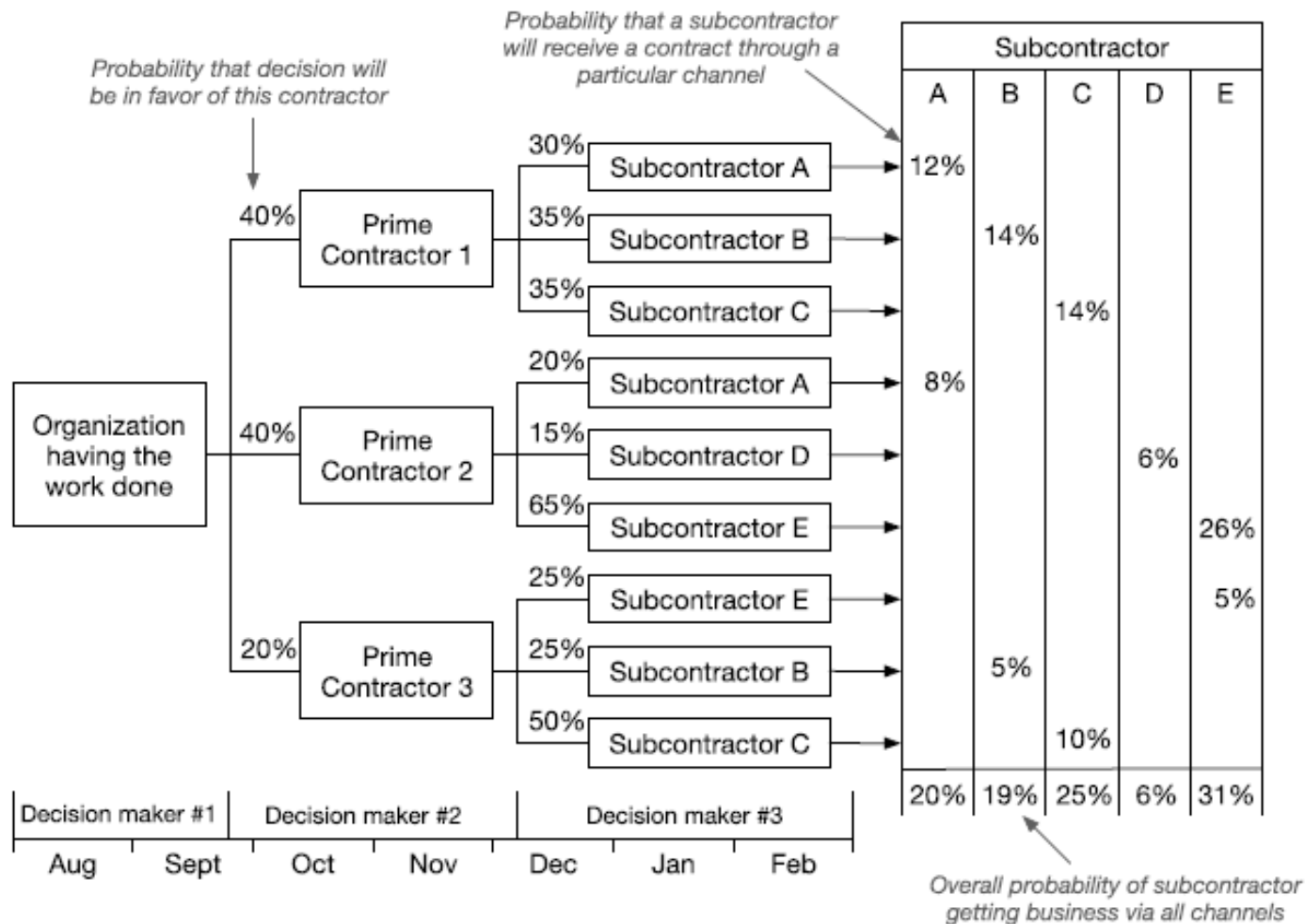


[Bertin, 1983]

side-by-side displays of (competing) results

# Qualitative Time-Oriented Data: Decision Chart

[Harris, 1999], [Time Viz, Aigner, et al., 2011]



side-by-side  
of competing  
results

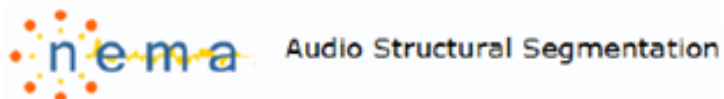
**Fig. 7.8:** Future decisions and corresponding alternative outcomes are depicted over time along with their probabilities.

Source: Adapted from Harris (1999).

# Qualitative Time-Oriented Data: Segmentation of Songs

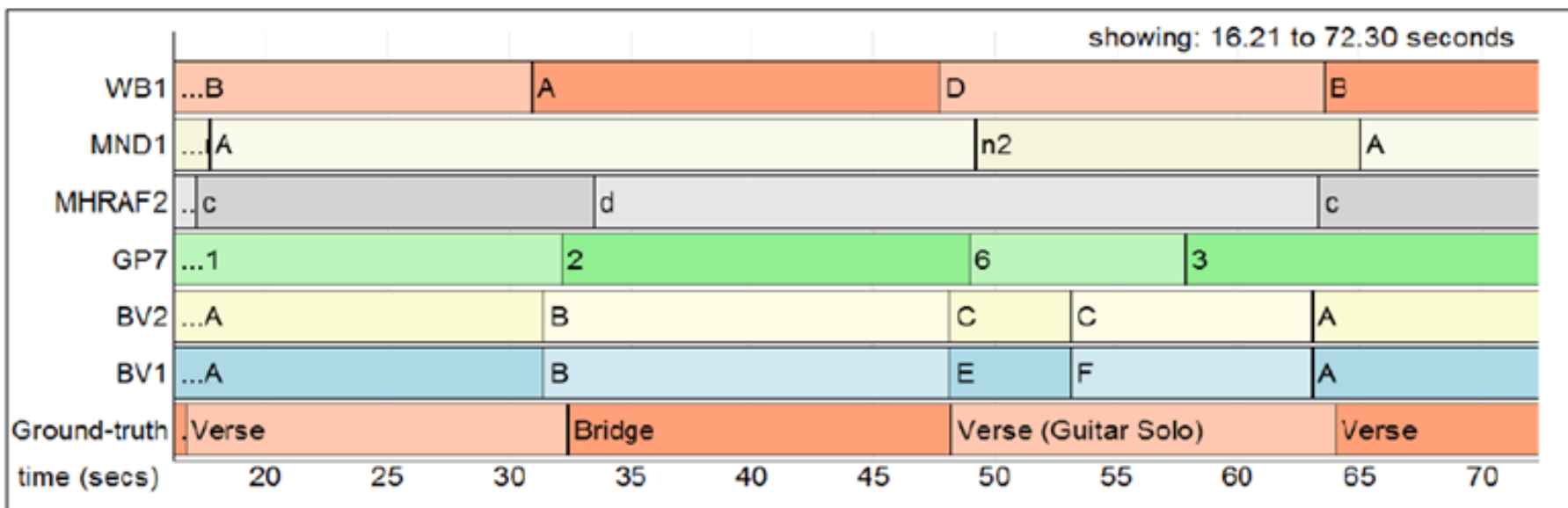
side-by-side of  
competing results

[<http://www.clir.org/pubs/reports/pub151/case-studies/salami>]



Comparative plots

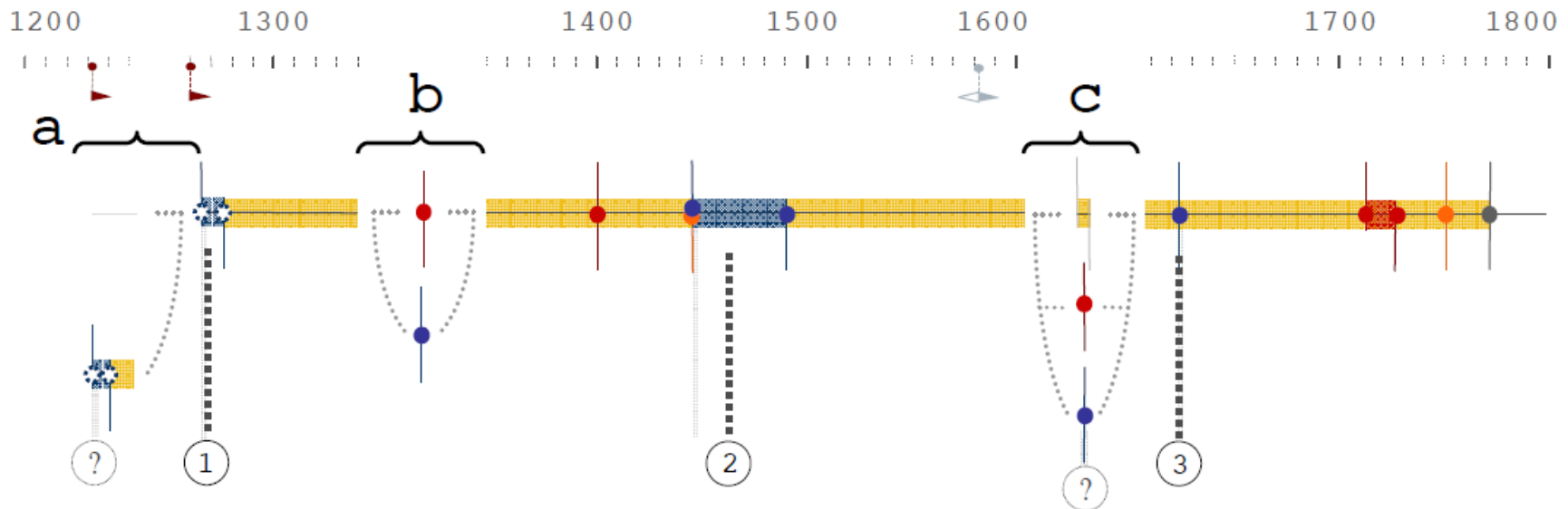
Structural segmentation for track struct\_mrx\_09\_000000 [\[top\]](#)



# Qualitative Time-Oriented Data: Multi-Hypothesis Chronology Diagram

side-by-side of  
competing results

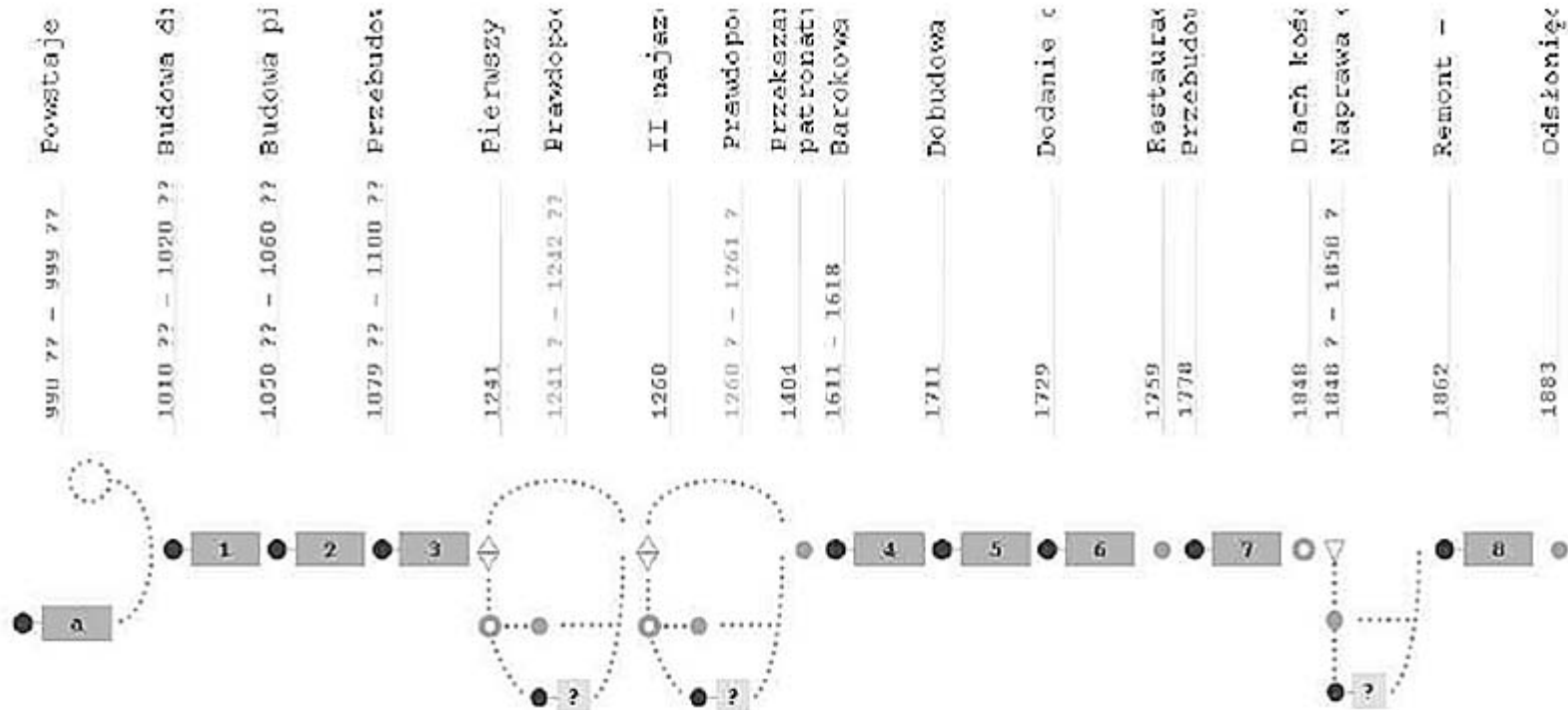
*[Dudek and Blaise, 2011]*





# Qualitative Time-Oriented Data: Graph of Potential Interactions

[Dudek and Blaise, 2011]



side-by-side of  
competing results

reliable  
transformations:  
proven by solid  
information

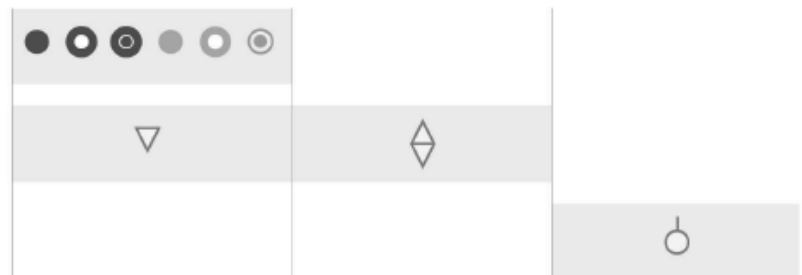
questionable  
transformations:  
the information does  
not prove it

contextual  
information:  
the information does  
not concern  
transformations

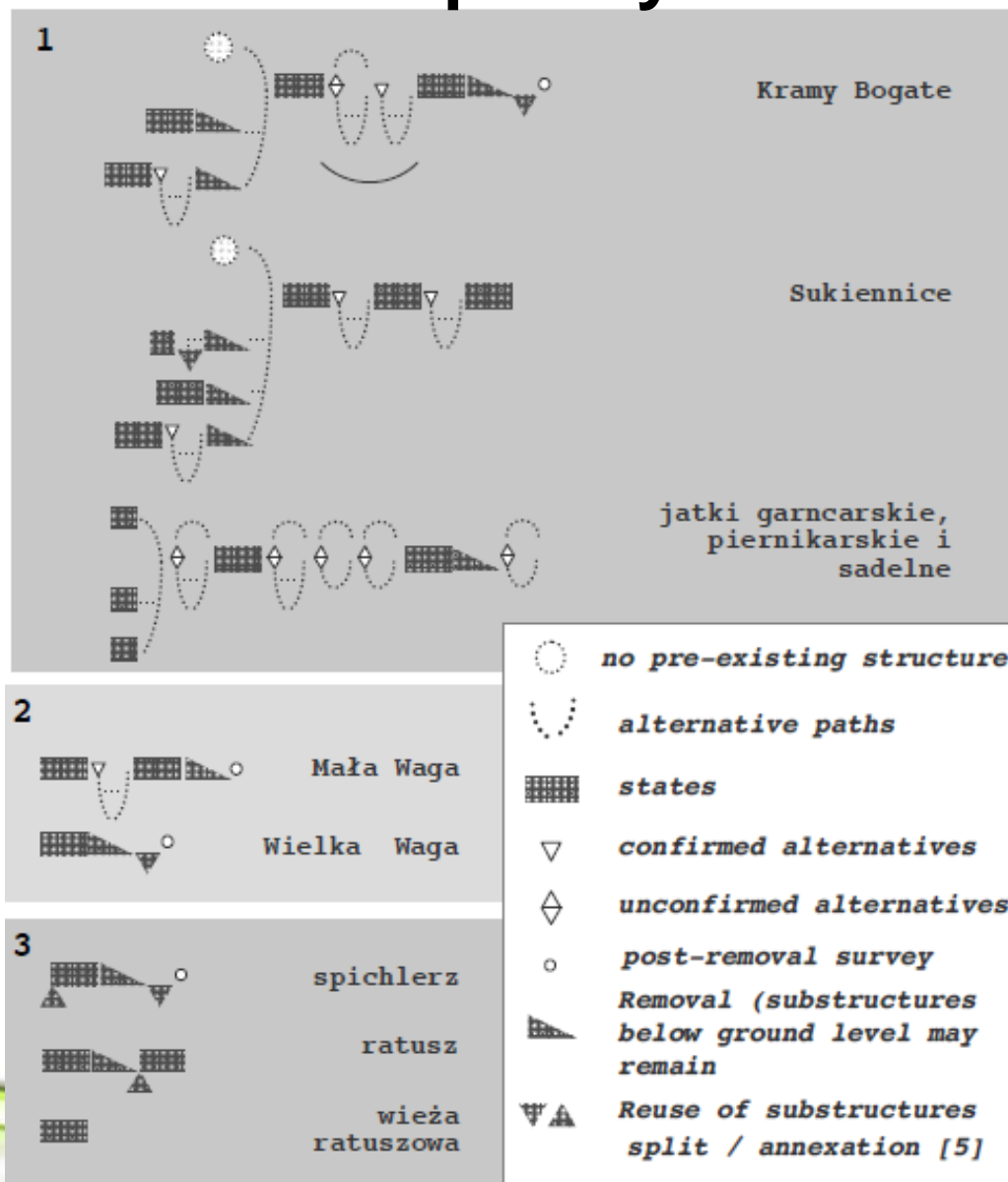
confirmed  
consequences

unclear  
consequences

no  
consequences



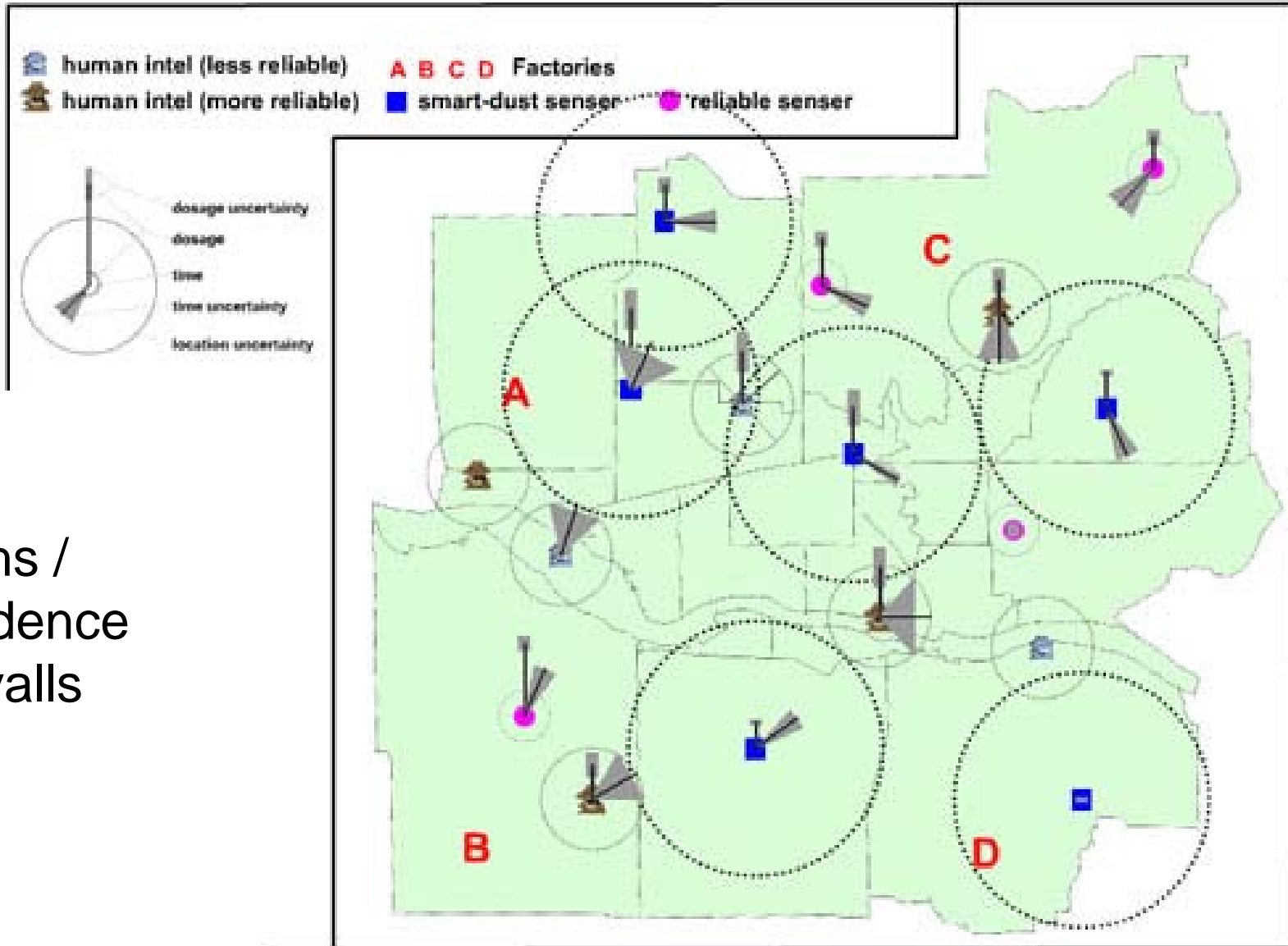
# Qualitative Time-Oriented Data: Visual Measure of Complexity

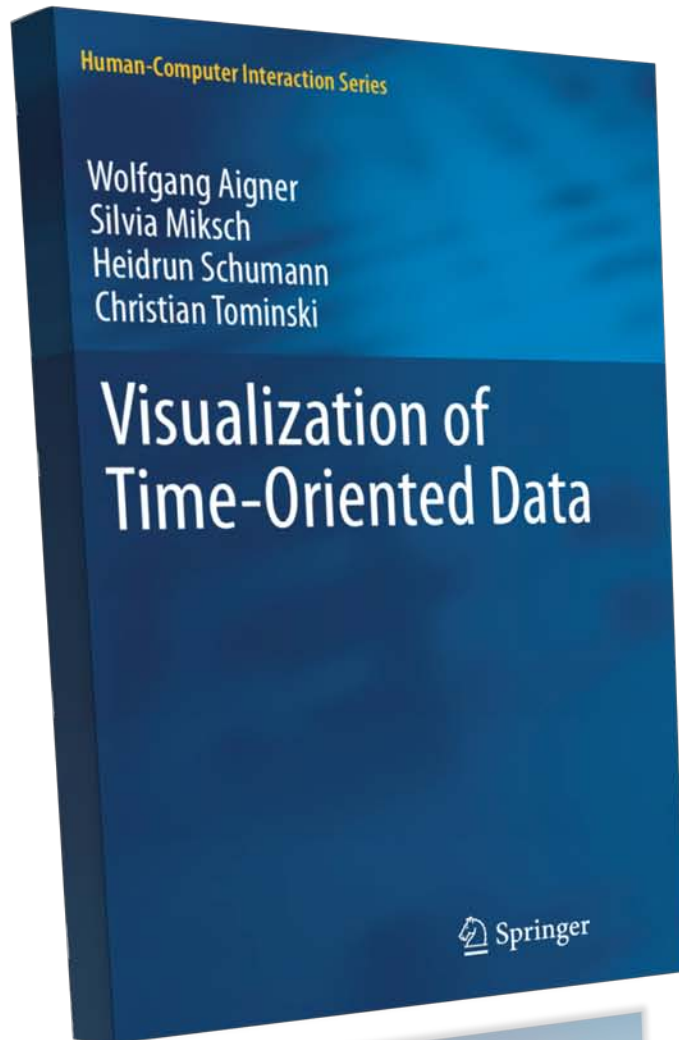


side-by-side  
of competing  
results

# Spatial, Temporal & Quantitative Uncertainty

[MacEachren et al., 2004]





Wolfgang Aigner • Silvia Miksch  
Heidrun Schumann • Christian  
Tominski

# Visualization of Time-Oriented Data

*with a foreword by Ben Shneiderman*

Springer

1st Edition, 2011, XVIII, 286 p. 221 illus., 198 in color.  
**Hardcover**, ISBN 978-0-85729-078-6.

## Table of Contents

Introduction • Historical Background •  
Time & Time-Oriented Data • Visualization Aspects •  
Interaction Support • Analytical Support •  
Survey of Visualization Techniques • Conclusion

**[www.timeviz.net](http://www.timeviz.net)**

# TimeViz Browser

## The TimeViz Browser

A Visual Survey of Visualization Techniques for Time-Oriented Data

# of Techniques: 101

Search:

### Data

#### Frame of Reference

- Abstract  ON
- Spatial  ON

#### Number of Variables

- Univariate  ON
- Multivariate  ON

### Time

#### Arrangement

- Linear  ON
- Cyclic  ON

#### Time Primitives

- Instant  ON
- Interval  ON

### Visualization

#### Mapping

- Static  ON
- Dynamic  ON

#### Dimensionality

- 2D  ON
- 3D  ON



The TimeViz Browser  
A Visual Survey of Visualization Techniques for Time-Oriented Data

# of Techniques: 101

Search:

Data

Frame of Reference

Abstract  ON

Spatial  ON

Number of Variables

Univariate  ON

Multivariate  ON

Time

Arrangement

Linear  ON

Cyclic  ON

Time Primitives

Instant  ON

Interval  ON

Visualization

Mapping

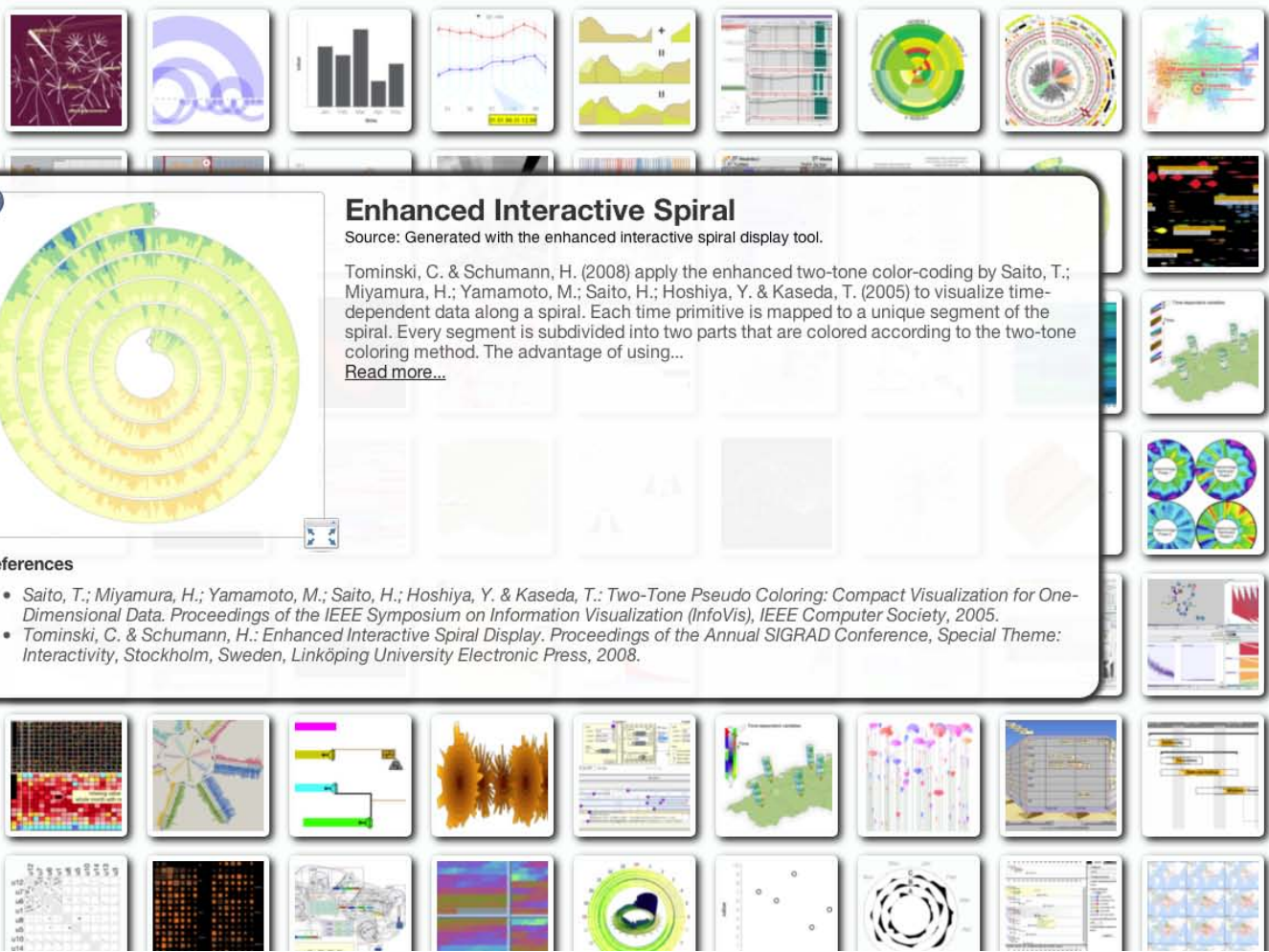
Static  ON

Dynamic  ON

Dimensionality

2D  ON

3D  ON



### Enhanced Interactive Spiral

Source: Generated with the enhanced interactive spiral display tool.

Tominski, C. & Schumann, H. (2008) apply the enhanced two-tone color-coding by Saito, T.; Miyamura, H.; Yamamoto, M.; Saito, H.; Hoshiya, Y. & Kaseda, T. (2005) to visualize time-dependent data along a spiral. Each time primitive is mapped to a unique segment of the spiral. Every segment is subdivided into two parts that are colored according to the two-tone coloring method. The advantage of using...

[Read more...](#)

#### References

- Saito, T.; Miyamura, H.; Yamamoto, M.; Saito, H.; Hoshiya, Y. & Kaseda, T.: *Two-Tone Pseudo Coloring: Compact Visualization for One-Dimensional Data*. Proceedings of the IEEE Symposium on Information Visualization (InfoVis), IEEE Computer Society, 2005.
- Tominski, C. & Schumann, H.: *Enhanced Interactive Spiral Display*. Proceedings of the Annual SIGRAD Conference, Special Theme: Interactivity, Stockholm, Sweden, Linköping University Electronic Press, 2008.

# Summary

Time has special characteristics

Temporal uncertainty mostly visualized by glyphs

Time-oriented data:

Quantitative -- qualitative

Abstract – spatial

Statistical uncertainty – bounded uncertainty

Need to further evaluate different methods to visually encode uncertainty



# Contact

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